



PRediction Of Geospace Radiation Environment and Solar wind parameters

Forecast of the radiation belt
environment

Moving average linear filters

- Find flux >2 MeV electrons based on Kp [[Nagai et al., 1988](#)]

Linear Prediction Filters

- Forecast high energy electrons using Kp, AE, and solar wind velocity [[Baker et al., 1990](#), [Vassiliadis et al., 2002](#)]

Neural Network

- Fluxes of >3 MeV electrons at GSO using ΣKp for 10 consecutive days [[Koons and Gorney, 1991](#)]

Empirical models

- [Li et al., 2001](#) - Radial diffusion \rightarrow diffusion multiplier
- [Ukhorskiy et al., 2004](#) - Dynamical nonlinear time series analysis + conditional probability of solar wind + magnetospheric inputs
- [Turner and Li, 2008](#) - Time delays between energy channels
- [Denton et al., 2015](#) - Flux probability distributions

Introduction

Two categories of codes forecasting the radiation environment

First principles codes

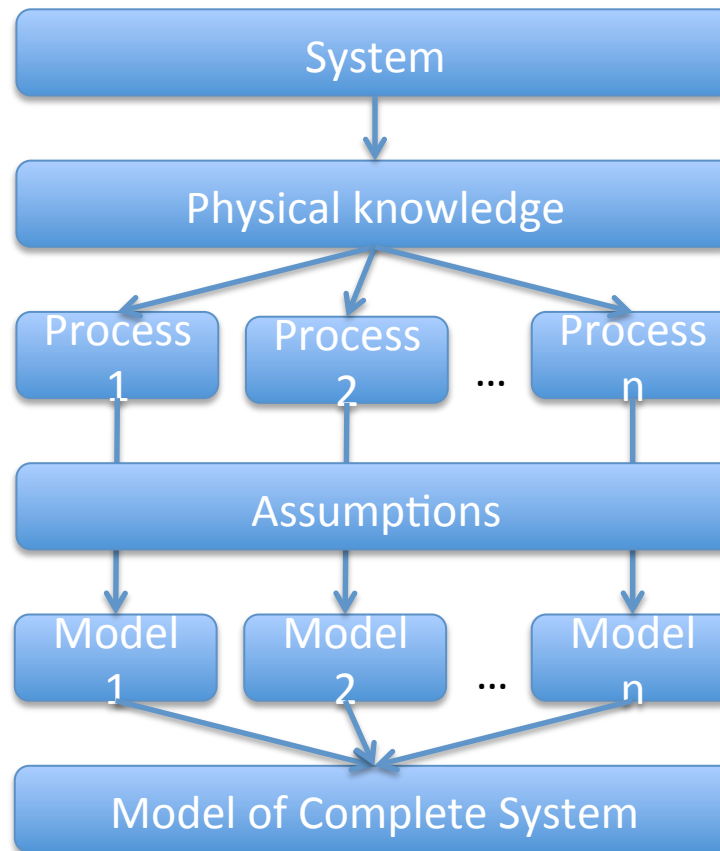
Individual processes modeled from first principles ,
Combine these sets of models to describe the dynamic evolution
of the environment. E.g. Versatile Electron Radiation Belt model

Empirical codes

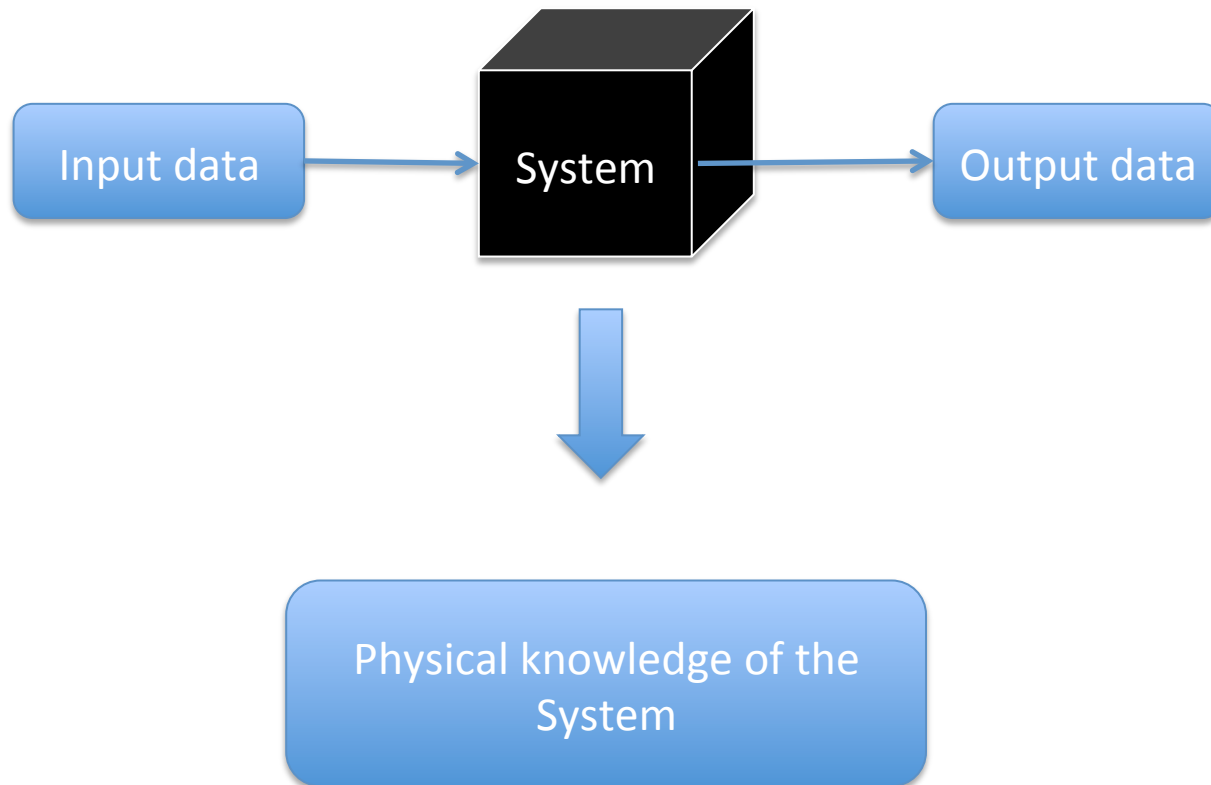
Based on systems science approaches,
Extracts information about processes occurring directly from
measurements. e.g. NARMAX

Both methods have their advantages and disadvantages.

First principles physical modeling



Systems Approach



Advantages/ Disadvantages

First Principles

Require knowledge of all processes occurring within a system

Known/modeled processes may be included/excluded to determine their relative effects

Require drivers
Eg boundary electron fluxes,
Geomagnetic activity eg Kp or Dst

Calculate electron fluxes in wide range of L-shell

Lower accuracy

Systems Analysis

Often there is minimal knowledge of the system

All processes modeled as one system

Role of input parameters

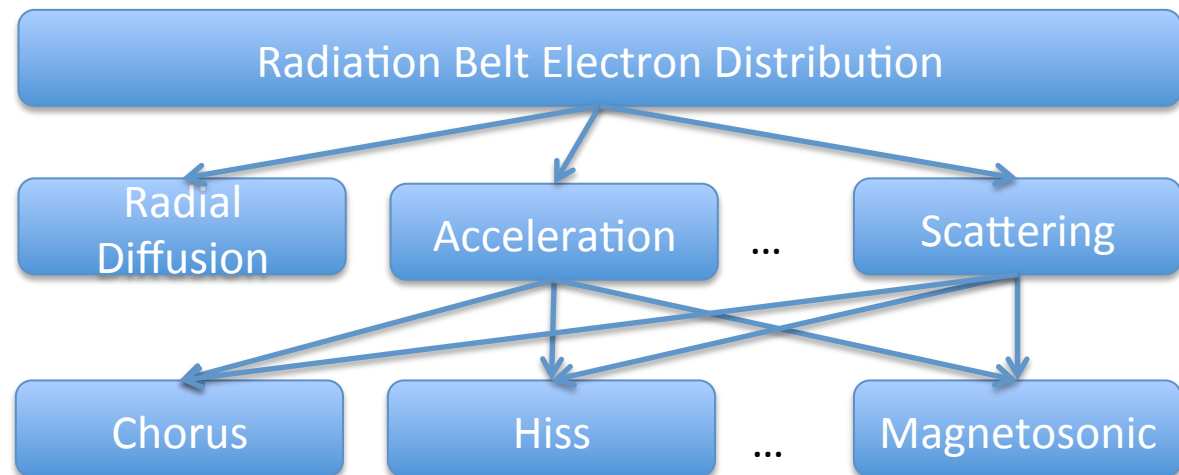
Require constant stream of input data
Only usable at geostationary orbit

Limited to region of high data density
eg GSO

Resulting models are currently the most accurate

VERB is a diffusion code that models radiation belt particle dynamics using the bounce averaged Fokker-Planck equation with radial, pitch angle and energy diffusion terms

Acceleration and scattering processes are incorporated in terms of diffusion coefficients resulting from the interaction of the particles with plasma waves such as Chorus, hiss, and magnetosonic.



Required inputs

- Kp – measure of geomagnetic activity
- Boundary flux – characterise inflow of particles from magnetotail

- VERB, the Versatile Electron Radiation Belt
- bounce averaged Fokker-Planck equation
- radial, pitchangle, energy, and mixed diffusion

$$\begin{aligned}
 \frac{\partial f}{\partial t} = & \underbrace{L^{*2} \frac{\partial}{\partial L^*} \Big|_{\mu, J} \left(D_{L^* L^*} L^{*-2} \frac{\partial f}{\partial L^*} \Big|_{\mu, J} \right)}_{\text{radial}} \\
 & + \frac{1}{p^2} \frac{\partial}{\partial p} \Big|_{y, L} \left(\underbrace{p^2 \langle D_{pp}(y, p) \rangle}_{\text{energy}} \frac{\partial f}{\partial p} \Big|_{y, L} + \underbrace{p^2 \langle D_{py}(y, p) \rangle}_{\text{mixed}} \frac{\partial f}{\partial y} \Big|_{p, L} \right) \\
 & + \frac{1}{T(y)y} \frac{\partial}{\partial y} \Big|_{p, L} \left(\underbrace{T(y)y \langle D_{yy}(y, p) \rangle}_{\text{pitchangle}} \frac{\partial f}{\partial y} \Big|_{p, L} + \underbrace{T(y)y \langle D_{yp}(y, p) \rangle}_{\text{mixed}} \frac{\partial f}{\partial p} \Big|_{y, L} \right) \\
 & - \frac{f}{\tau}, \tag{1}
 \end{aligned}$$

- Violation of third adiabatic invariant
- Transport particles into regions of increased or decreased magnetic field
- Associated with increase or decrease in particle energy respectively
- VERB uses time dependent radial diffusion based on Kp index (Brautigan and Albert 2000)

Energy/pitchangle diffusion

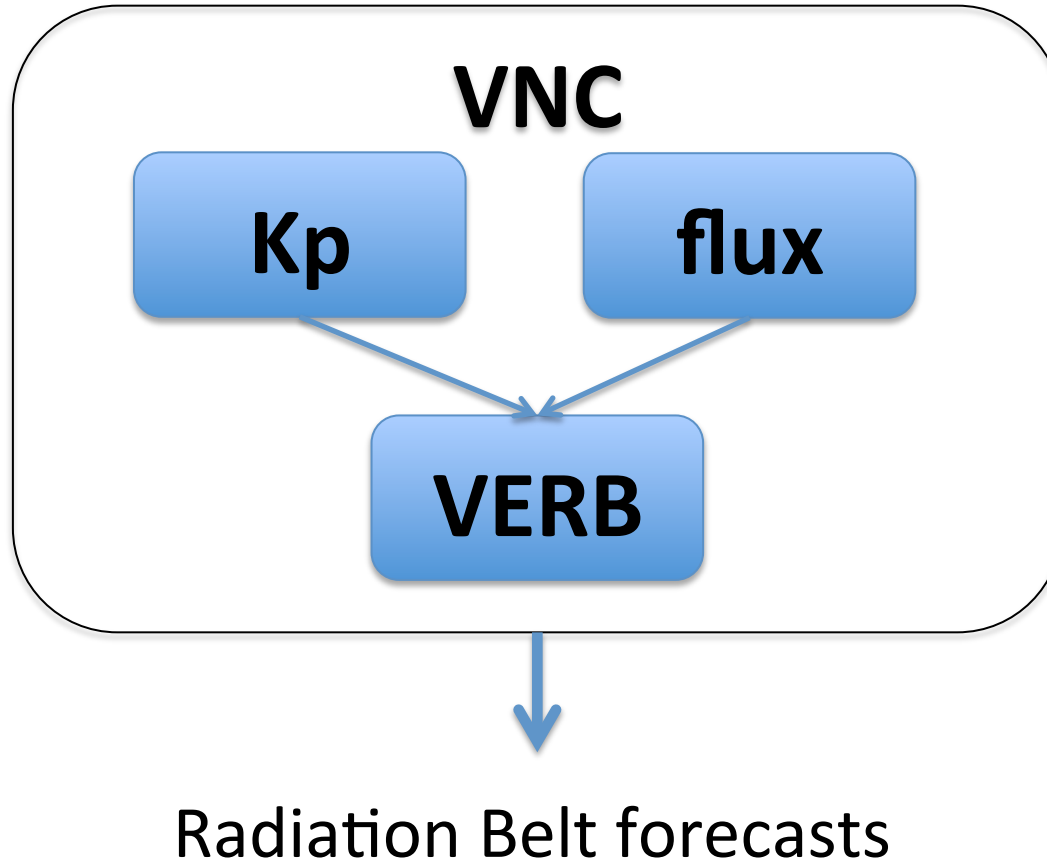
- Interaction with localised plasma waves results in diffusion in energy and pitchangle
- Diffusion coefficients estimated from observations of the variation in wave mode amplitude as a function of location, geomagnetic activity

Solve Fokker-Planck equation for

- Radial distance $1 < L^* < 7$
- Energy 0.01-10 MeV at $L^* = 7$
- Pitch angle 0-90 degrees

Boundary	Condition	Explanation
$E = E_{\min}$	$f = \text{const}$	Balance of convective source and losses
$E = E_{\max}$	$f = 0$	Absence of high-energy electrons at multi-MeV energies
$\alpha_0 = 0^\circ$	$f = 0$	Empty loss cone in the weak diffusion regime
$\alpha_0 = 90^\circ$	$\partial F / \partial \alpha_0 = 0$	Flat pitch angle distribution at 90°
$L = 1$	$f = 0$	Losses to atmosphere measurements
$L = 7$	$f = f(\text{time})$	

- SNB³GEO is the Sheffield NARMAX model for forecasts of electron fluxes at GEO
- Models for >2MeV, >800keV, 475keV, 275keV, 150keV, 75keV, 40keV
- Overview plots -
https://sbg.group.shef.ac.uk/progress/html/narmax_results.phtml
- Models provide the most accurate forecasts of these fluxes, better than NOAA REFM



The VERB-NARMAX-Coupled model attempts to integrate these two different yet complementary approaches **for past/fore-casting**.

NARMAX

- Used to model measurements of electron fluxes at GEO based on data from GOES 13
- Provide a 24hr ahead forecast of electron fluxes at GEO

Model forecasts at GEO ($L^* \sim 6.2$) are used to estimate the outer boundary fluxes at $L^* = 7$ that are used by VERB

VERB

- Used to model the dynamics of the radiation belts based on estimated fluxes and K_p

Measurements (GOES 13, 15) and forecasts (SNB³GEO) provide electron fluxes

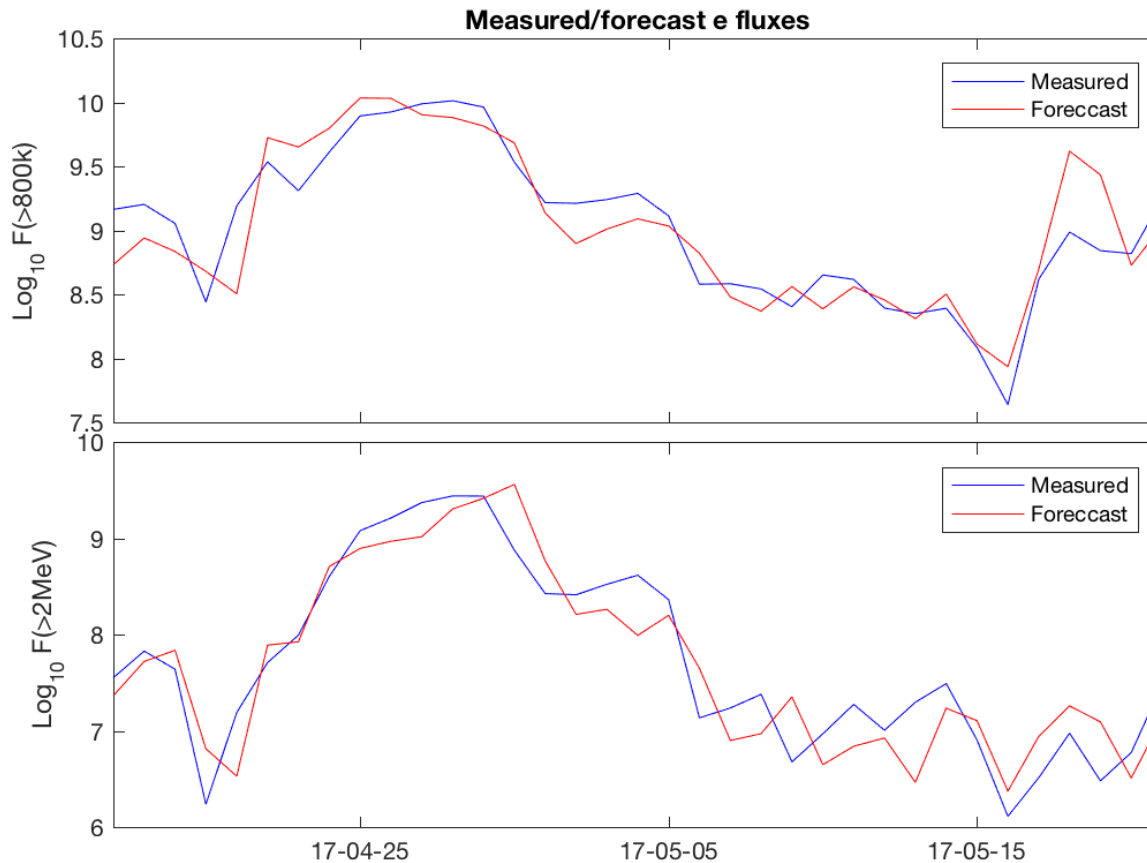
- Energy range: >2MeV and >800 keV
- Radial distance: $L \sim 6.6$ (GEO)

VERB initialised using electron flux

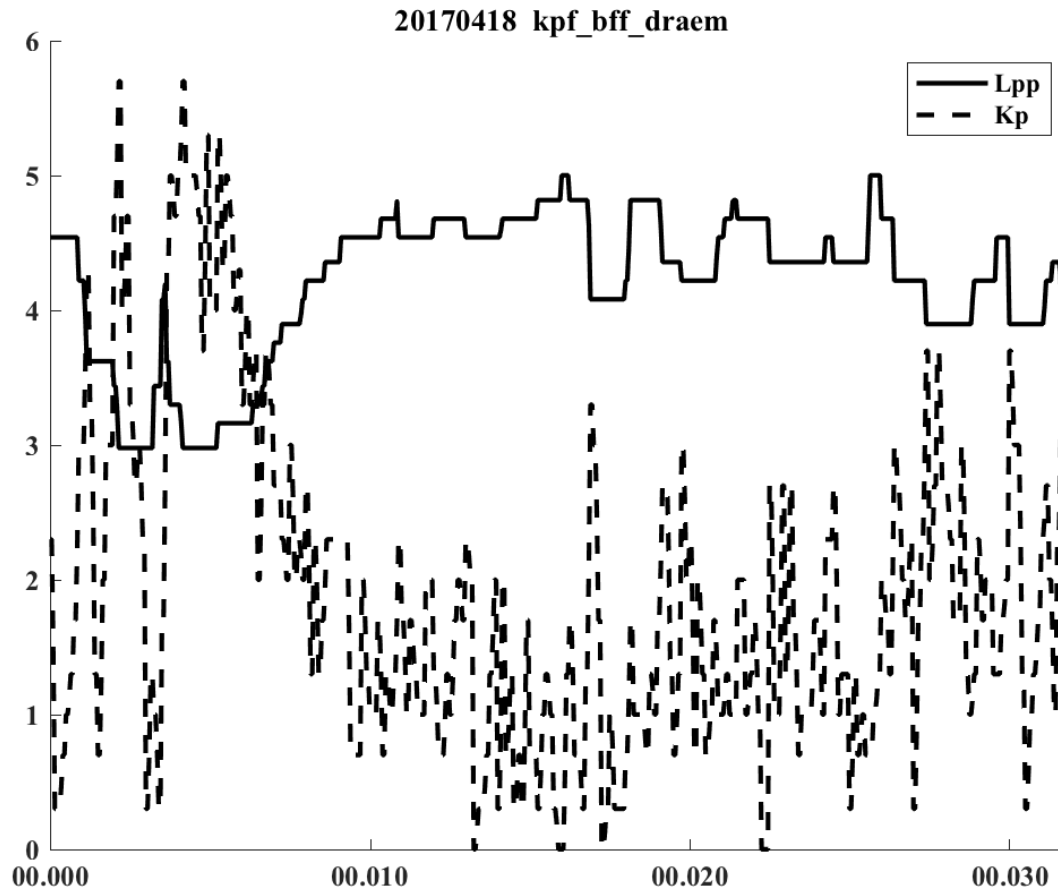
- Energy: 900 keV
- Radial distance: $L^* = 7$

Assume

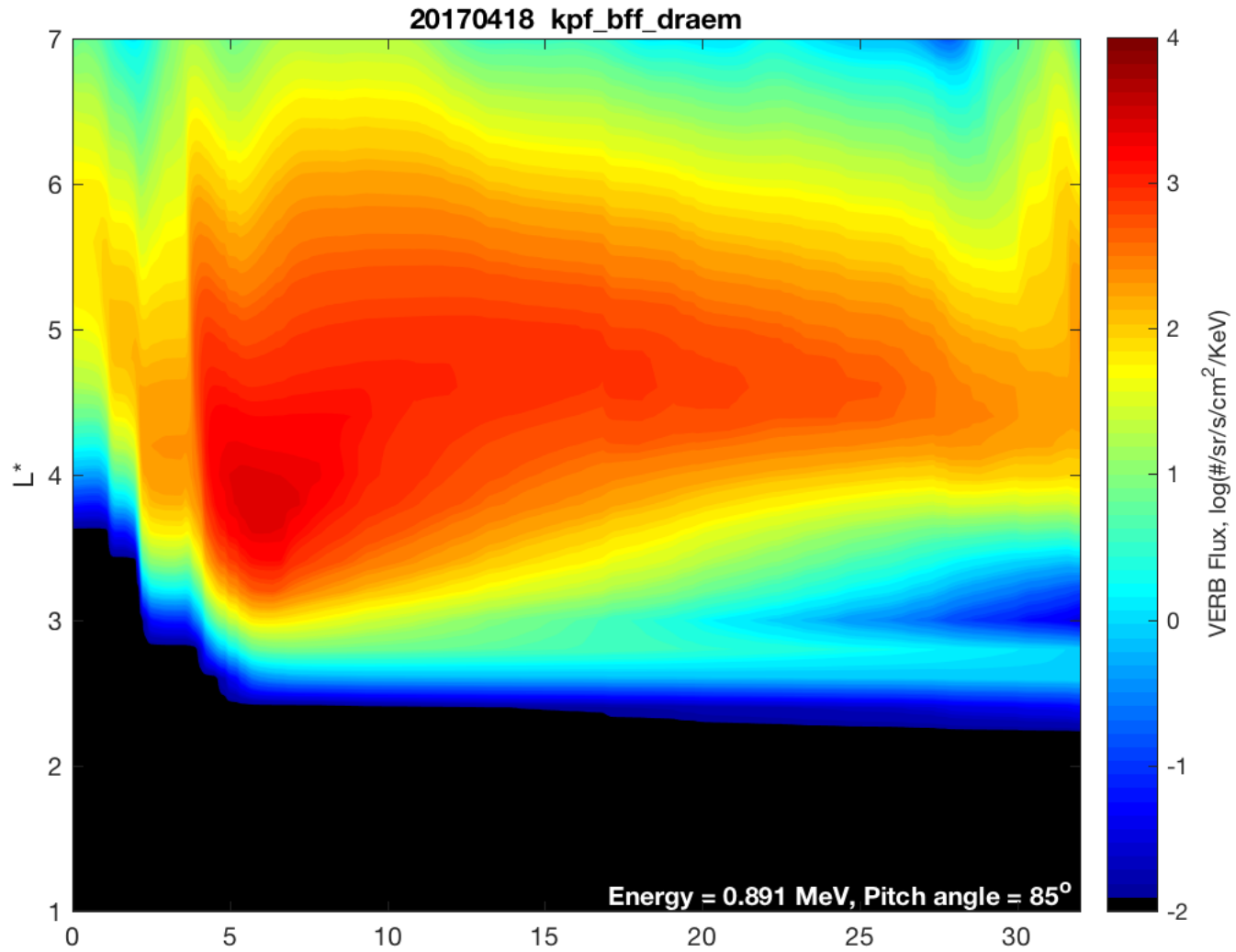
- Average L^* for GEO is 6.2
- Phase Space Density of particles does not vary significantly between $L^*=6.2$ and $L^*=7$

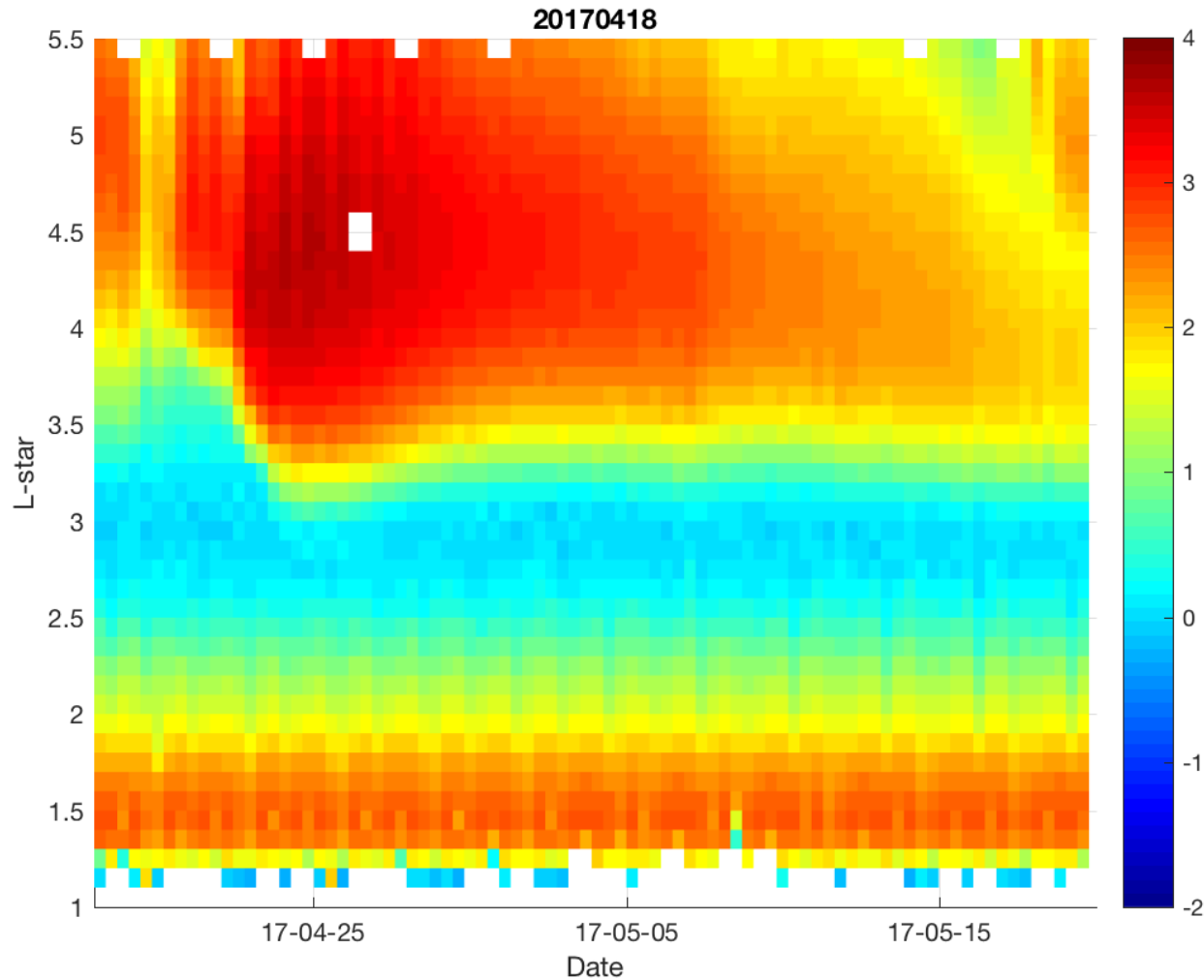


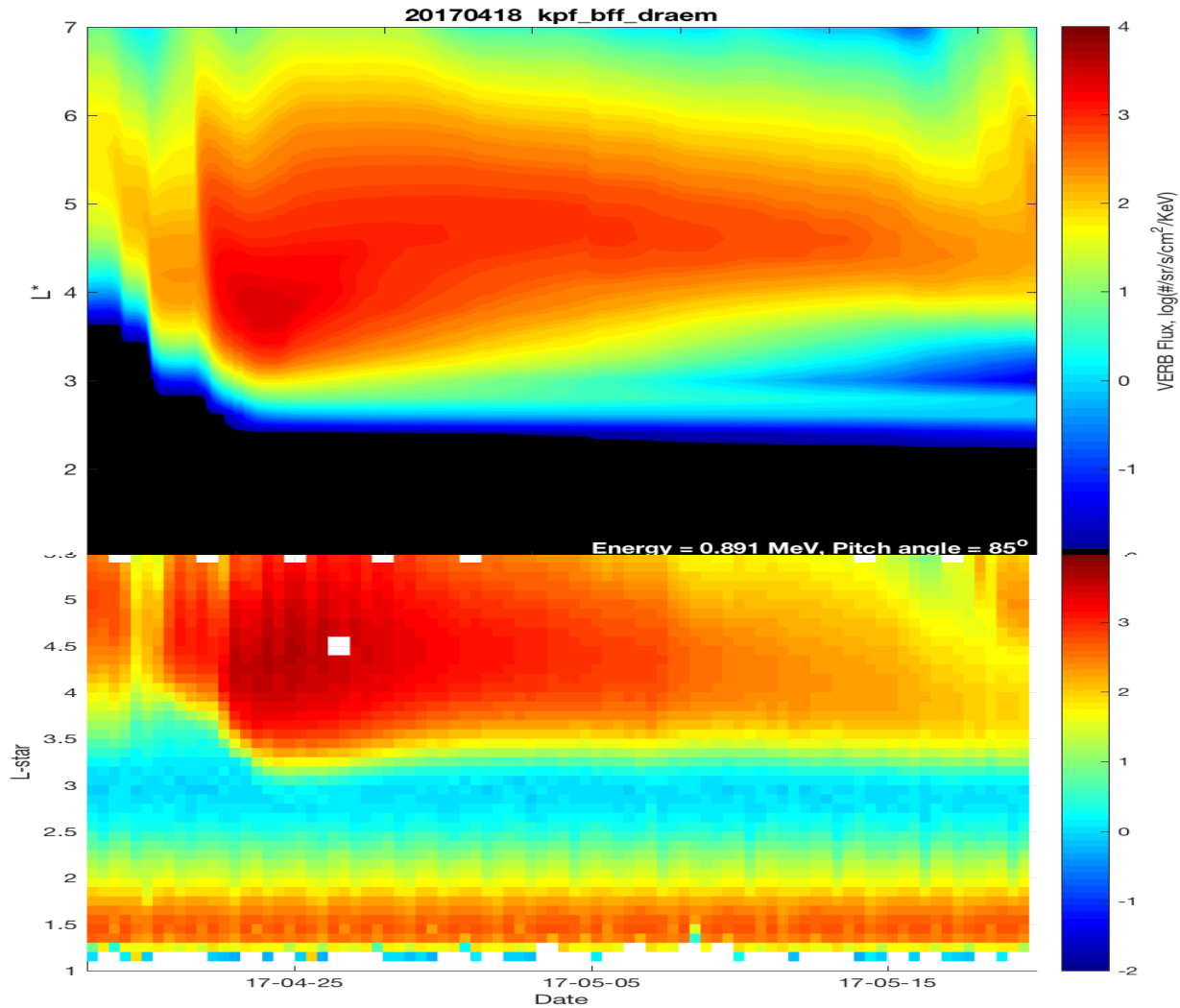
Input - Kp



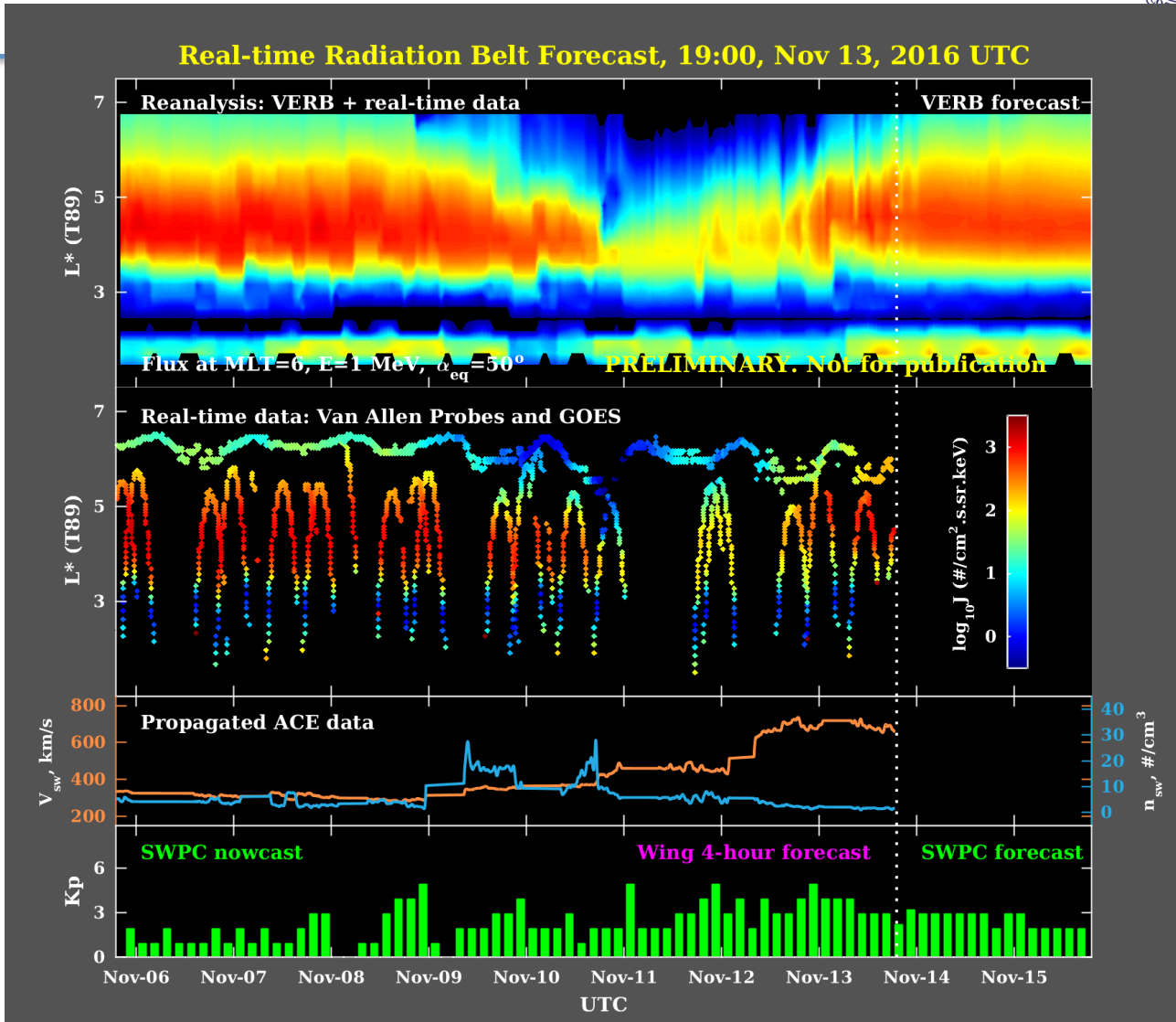
VERB results







VERB



Coupling of the VERB first principles and NARMAX systems models

- NARMAX was used to forecast daily fluxes of $>800\text{keV}$ and $>2\text{Mev}$ electrons at GEO
- These fluxes were used to estimate the input boundary fluxes required by VERB
- VERB was then used to simulate the electron fluxes for entire radiation belt region
- Qualitatively, the results reproduce measurements from the Van Allen Probes MagEIS instrument



PRediction Of Geospace Radiation Environment and Solar wind parameters

Fusion of tools

Objectives

- Collect and implement models for geomagnetic index forecast at Sheffield and provide access to their forecasts via project web page.
- To provide access to the forecasts of models developed in WP 4 via the project web page.
- To implement the VERB-NARMAX and VERB-IMPTAM models, developed in WP 5 and 6 at USFD, and provide access to their forecasts via the project web page.
- Develop a tool to calculate the integrated electron fluxes along a user defined part of satellite orbit
- Implement a traffic light system and create an email circular summarising current and evolution of space weather conditions.

Project website has a results menu

Results

Geomagnetic indices	[+]
Electron Flux forecasts	[+]
Statistical wave models	

Geomagnetic indices

- Lund Kp (WP 3)
- Lund Dst (WP 3)

Electron fluxes

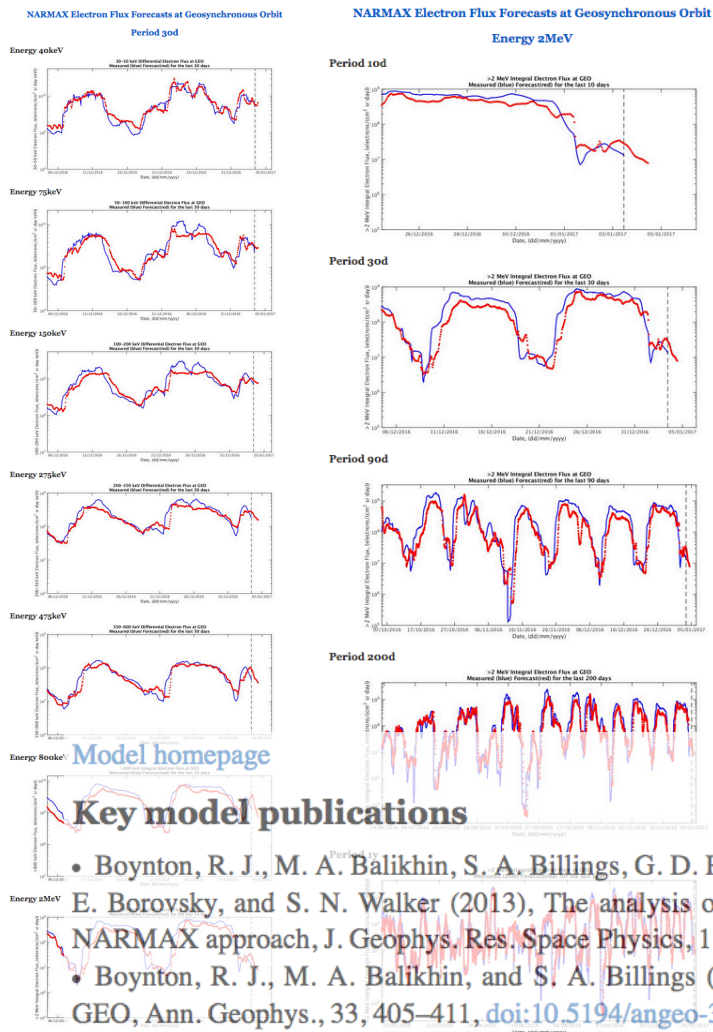
- NARMAX GEO fluxes (WP 6)
- IMPTAM low energy electrons (WP 5)
- VERB high energy electrons (WP 6)

Statistical wave models

- Chorus
- Hiss

Results

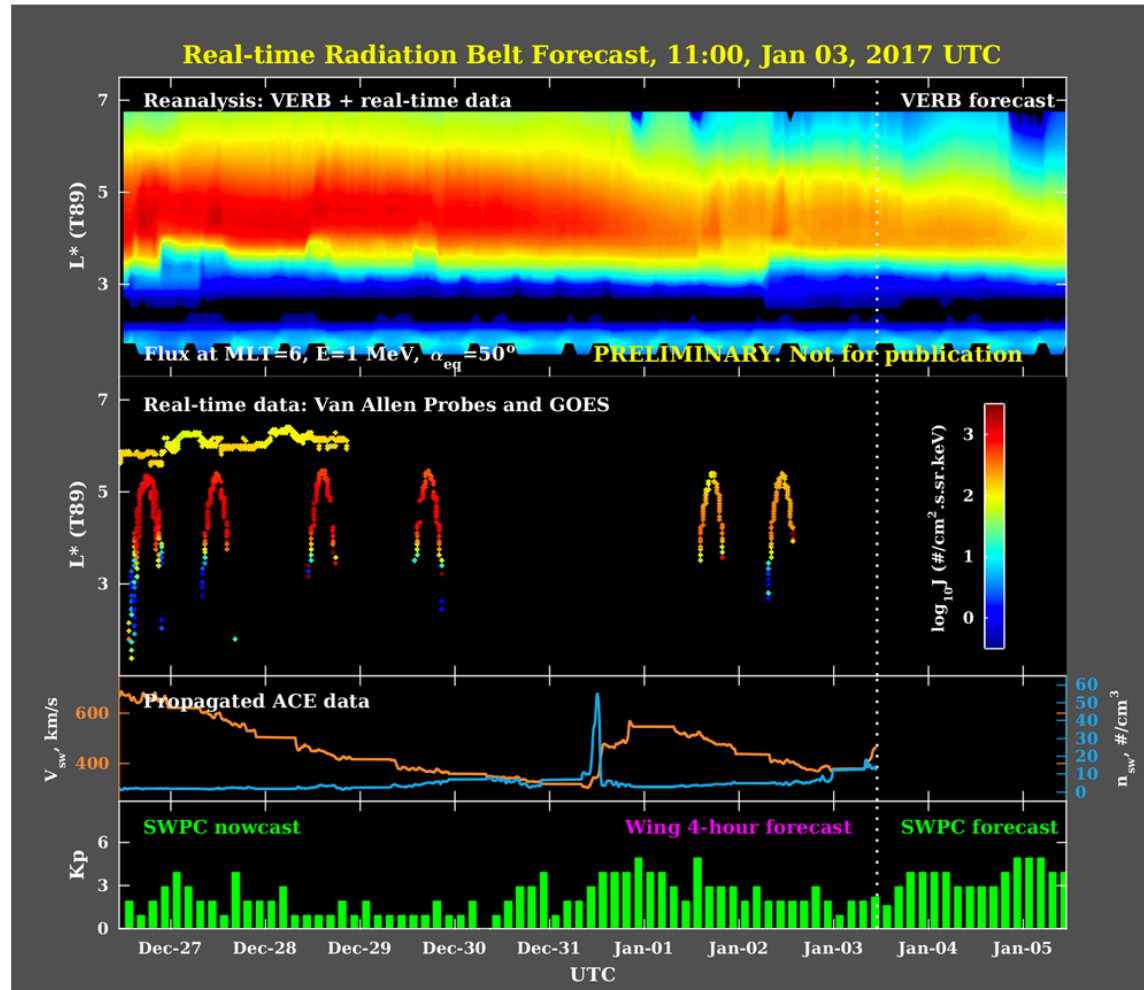
Geomagnetic indices	[+]
Electron Flux forecasts	[-]
NARMAX	[-]
Periods	[-]
10 days	
30 days	
90 days	
200 days	
1 year	
Energies	[-]
2MeV	
800keV	
475keV	
275keV	
150keV	
75keV	
40keV	
IMPTAM	[+]
VERB	[+]

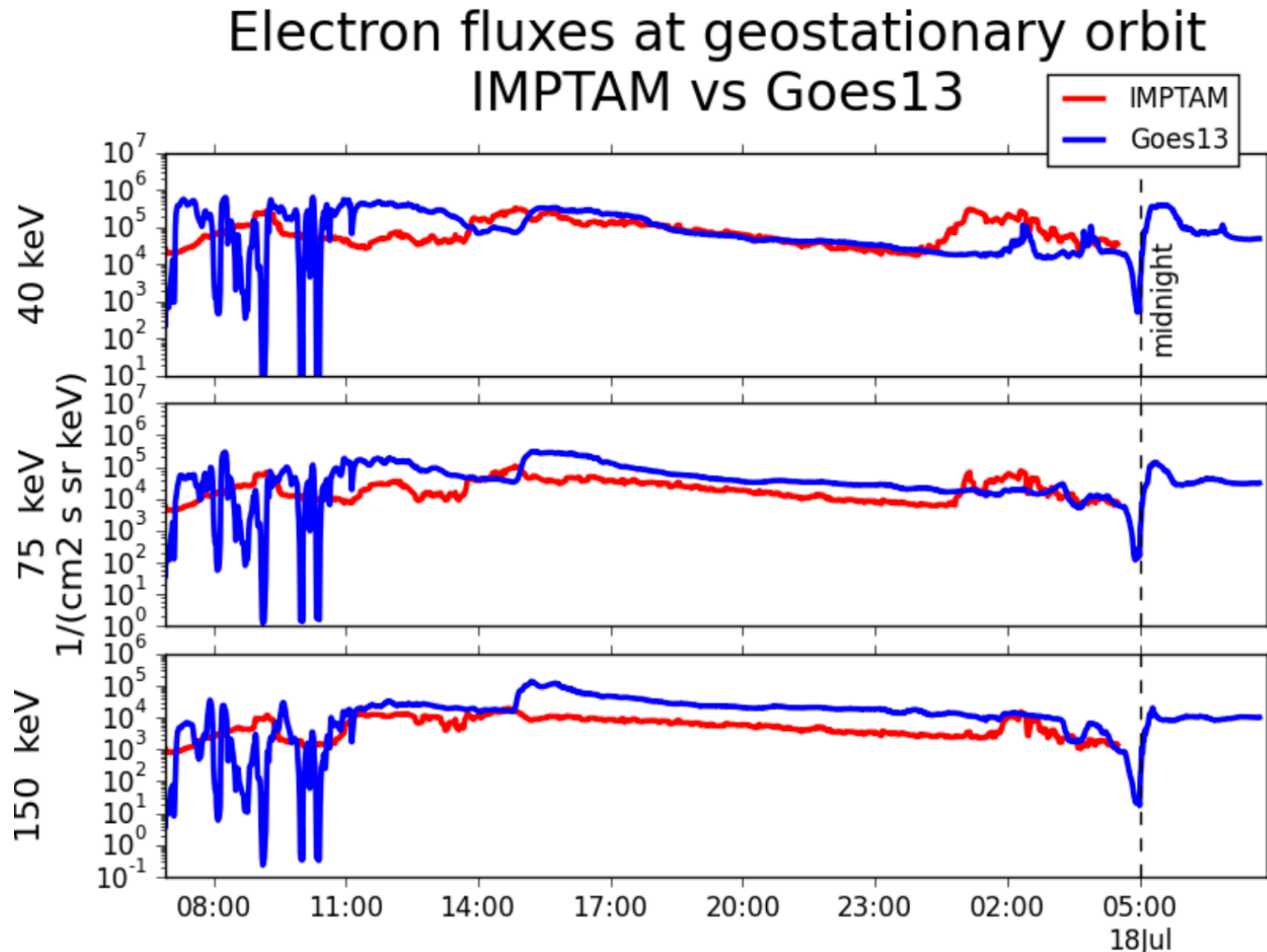


NARMAX GEO e- fluxes

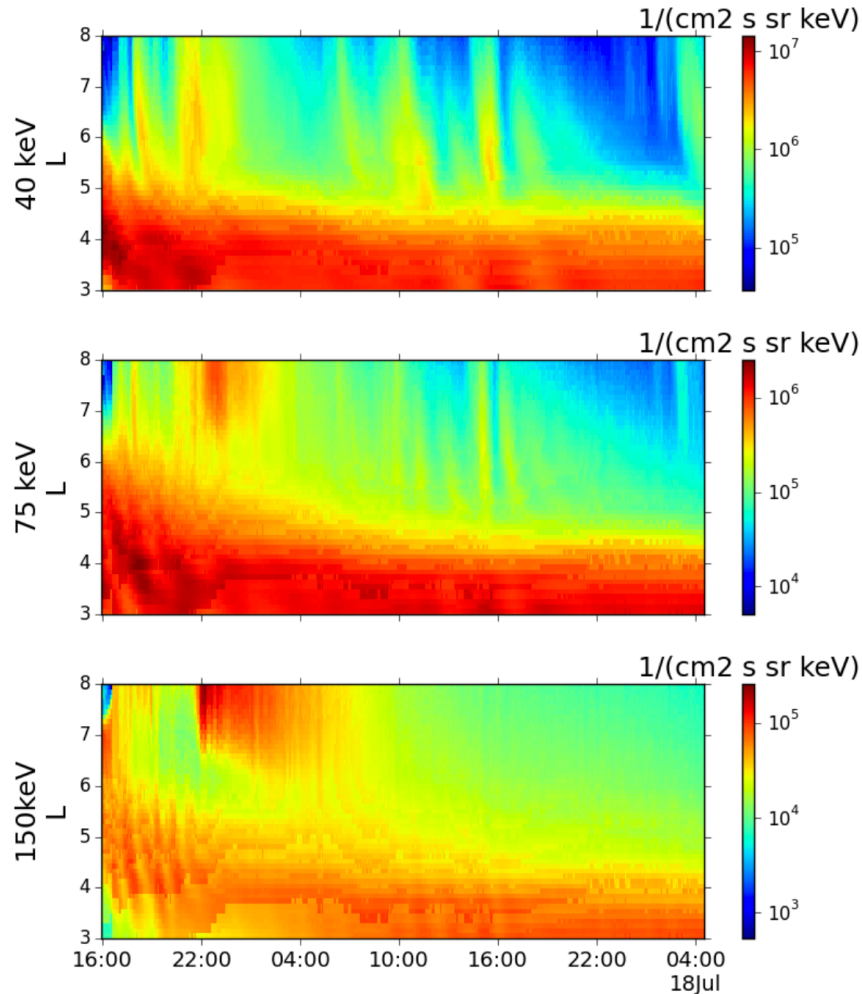
- Menu
- Forecasts v measured fluxes for past #days, all energies
- Forecasts v measured fluxes for single energy over various time periods
- Model information

VERB Radiation Belt Nowcast and Forecast

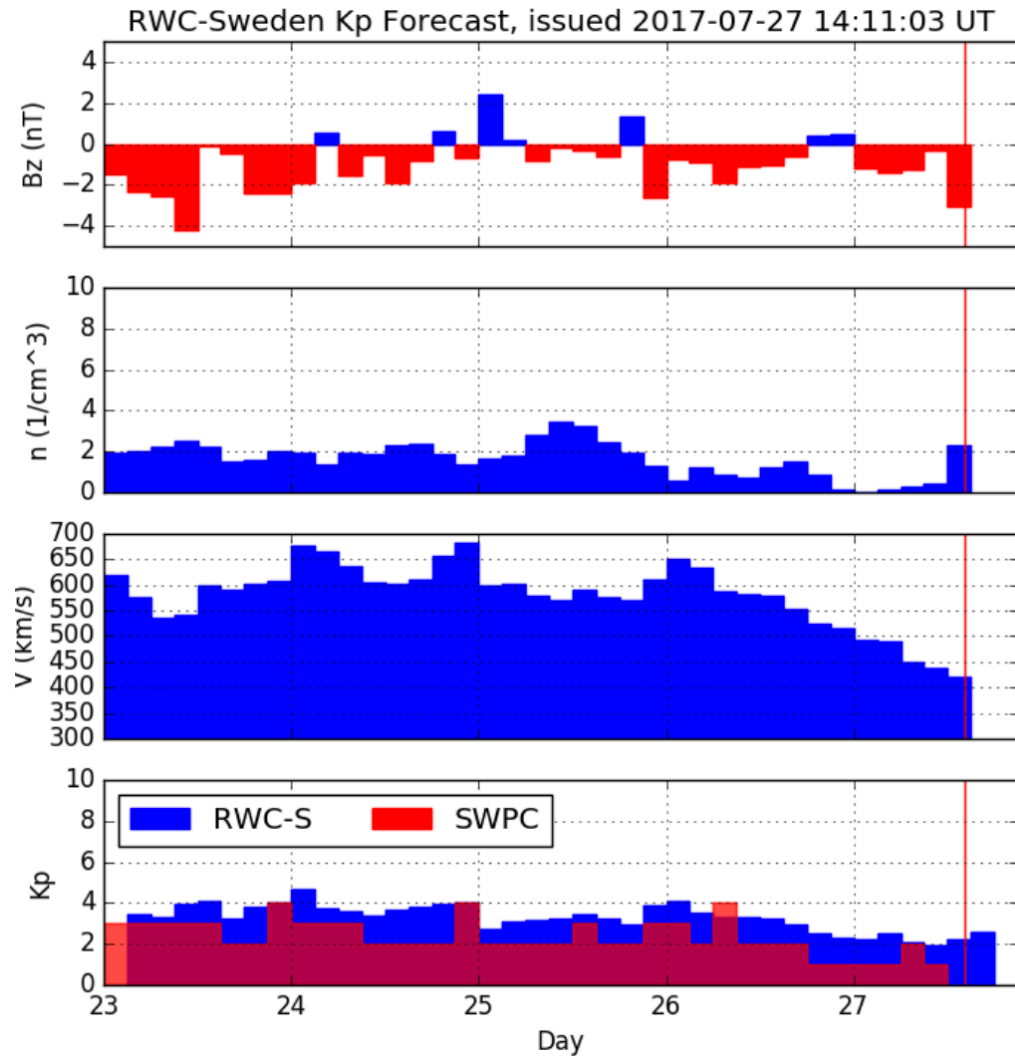




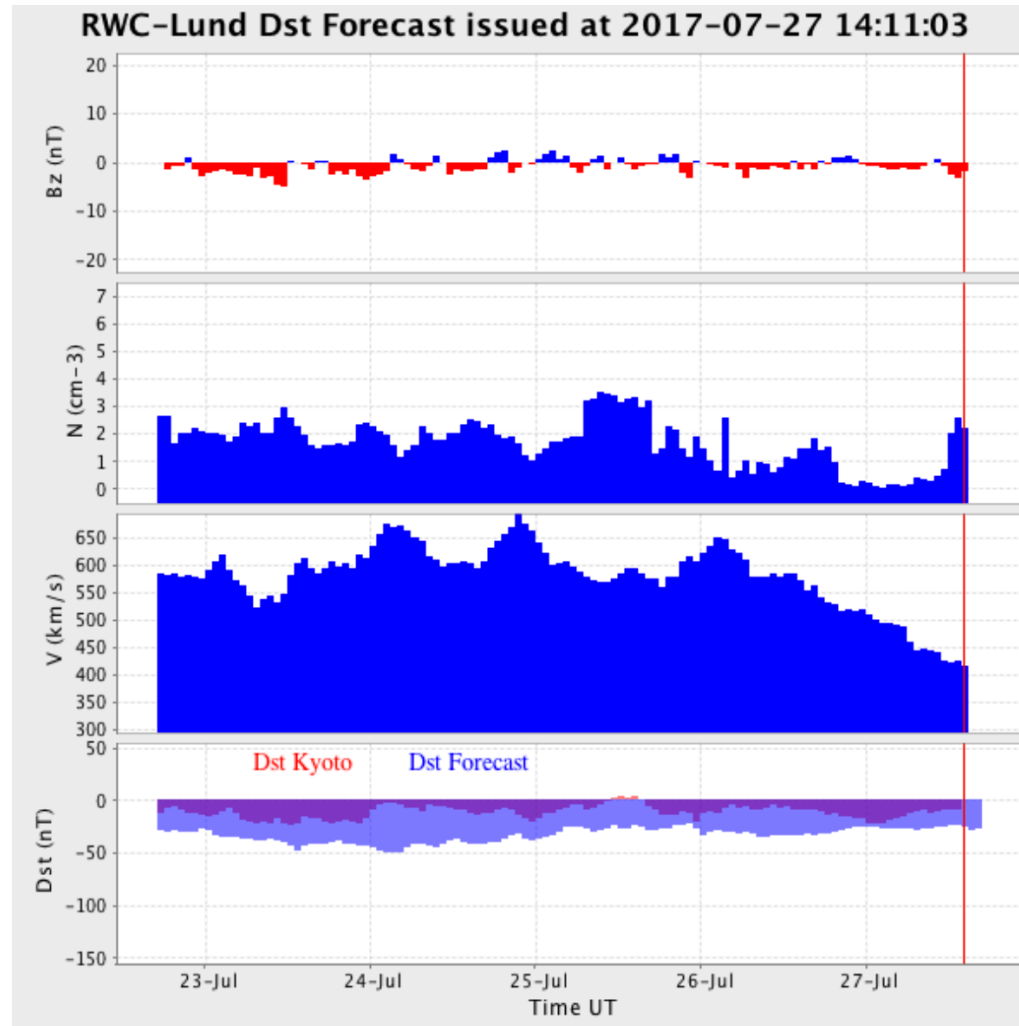
IMPTAM electron fluxes at midnight



Lund Kp



Lund Dst



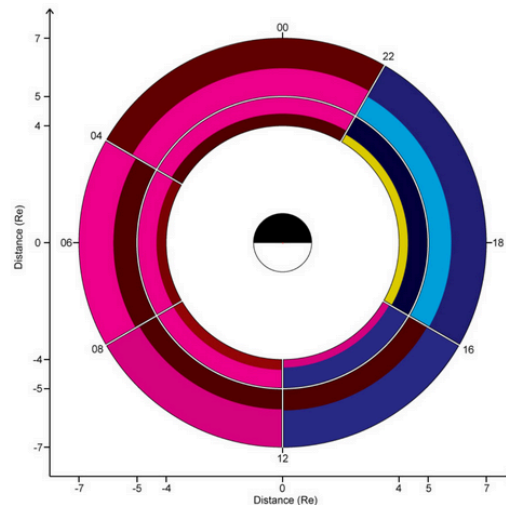
Statistical Wave Models

Magnetic field wave data from the Cluster and THEMIS missions has been used as the basis to compute new statistical wave models for the amplitudes of lower band chorus, hiss, and equatorial magnetosonic waves. The models are based on the results of an Error Reduction Ratio analysis of solar wind parameters, location, and geomagnetic indices in order to determine which of the input set of parameters are in most influential of the evolution of the magnetic field amplitudes of the wave modes under consideration.

- [Description of the Error Reduction Analysis and it application](#)
- [Description of the calculation of the Statistical Wave Models](#)
- [Download the set of Statistical Wave Models](#)

Lower band chorus

[Download the set of LBC wave models](#)



Time lag (hours) LBC	1	2	3	4	5	6	7	8	9	10
Velocity	Red	Red	Red	Red	Red	Red	Red	Red	Red	Red
Density	Yellow	Yellow	Yellow	Yellow	Yellow	Yellow	Yellow	Yellow	Yellow	Yellow
Pressure	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
IMF Factor	Blue	Blue	Blue	Blue	Blue	Blue	Blue	Blue	Blue	Blue
Dst Index	Dark Blue	Dark Blue	Dark Blue	Dark Blue	Dark Blue	Dark Blue	Dark Blue	Dark Blue	Dark Blue	Dark Blue
AE Index	Pink	Pink	Pink	Pink	Pink	Pink	Pink	Pink	Pink	Pink

Notes:

None

New developments, currently on the test web site

Current space weather conditions (WP 7)

Shows current (and forecast) values for

- geomagnetic indices
- various solar wind parameters
- GEO electron fluxes

Current Conditions

Magnetosphere Current Forecast

Dst (nT)	0
Kp	7

Solar wind Current Forecast

B (nT)	3.8
Bz (nT gsm)	-1.5
Density (cm ⁻³)	4.7
Velocity (kms ⁻¹)	334.2

GEO e⁻ flux Current Forecast

F>2MeV	8.829	8.553
F>800keV	9.7006	9.3311

Geomagnetic indices

Dst – WDC Kyoto

Kp – GFZ Potsdam

Solar wind

All data from ACE real time

GEO electron flux

GOES observations

Sheffield NARMAX models