



VNC: Application of Physics and Systems Science methodologies to Forecasting of the Radiation Belt Electron Environment

S. N. Walker¹, M. A. Balikhin¹, I.
Pakhotin^{1,2}, and Y. Shprits²

¹ ACSE, University of Sheffield, U.K.,

² Now at University of Alberta, Canada

³ GFZ, Potsdam, Germany

Two categories of codes forecasting the radiation environment

First principles codes

Individual processes modeled from first principles ,
Combine these sets of models to describe the dynamic evolution of the environment. E.g. Versatile Electron Radiation Belt model

Empirical codes

Based on systems science approaches,
Extracts information about processes occurring directly from measurements.
E.g. NARMAX

Both methods have their advantages and disadvantages.

Moving average linear filters

- Find flux $>2\text{Mev}$ electrons based on Kp [[Nagai et al., 1988](#)]

Linear Prediction Filters

- Forecast high energy electrons using Kp, AE, and solar wind velocity [[Baker et al., 1990](#), [Vassiliadis et al., 2002](#)]

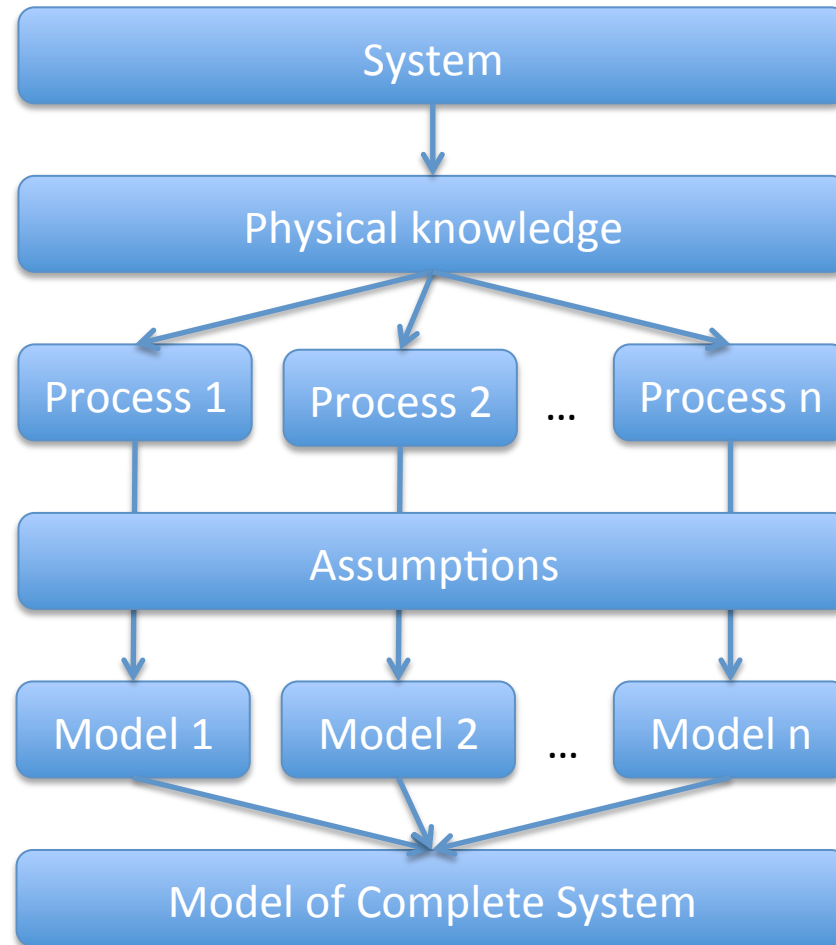
Neural Network

- Fluxes of $>3\text{MeV}$ electrons at GSO using ΣKp for 10 consecutive days [[Koons and Gorney, 1991](#)]

Empirical models

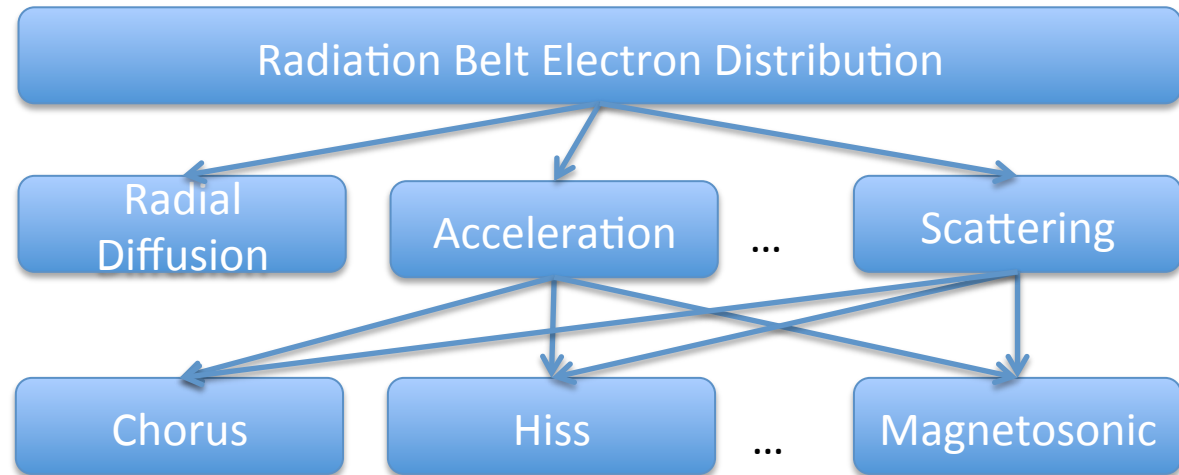
- [Li et al., 2001](#) - Radial diffusion \rightarrow diffusion multiplier
- [Ukhorskiy et al., 2004](#) - Dynamical nonlinear time series analysis + conditional probability of solar wind + magnetospheric inputs
- [Turner and Li, 2008](#) - Time delays between energy channels
- [Denton et al., 2015](#) - Flux probability distributions

First Principles Model



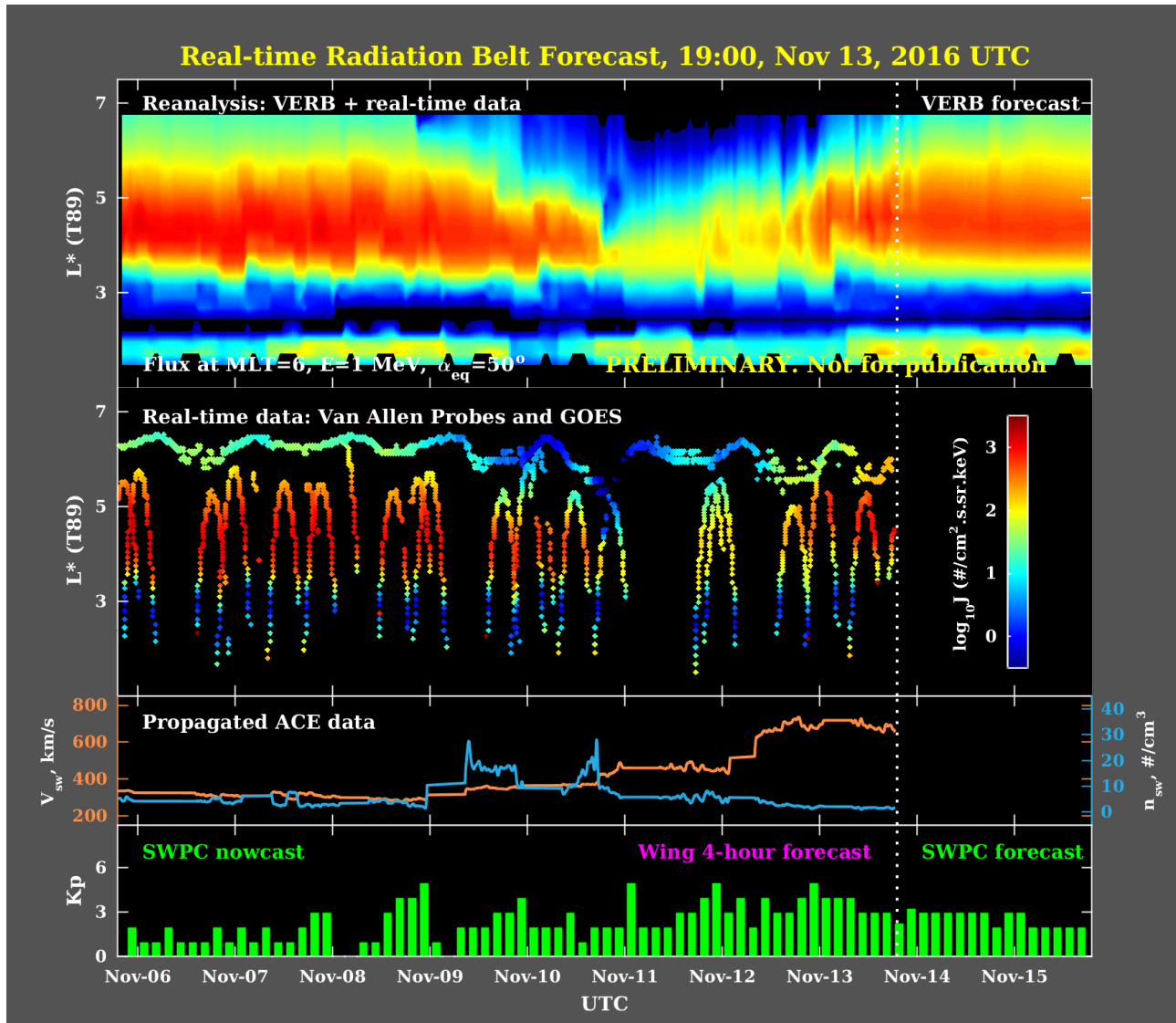
VERB is a diffusion code that models radiation belt particle dynamics using the bounce averaged Fokker-Planck equation with radial, pitch angle and energy diffusion terms

Acceleration and scattering processes are incorporated in terms of diffusion coefficients resulting from the interaction of the particles with plasma waves such as Chorus, hiss, and magnetosonic.

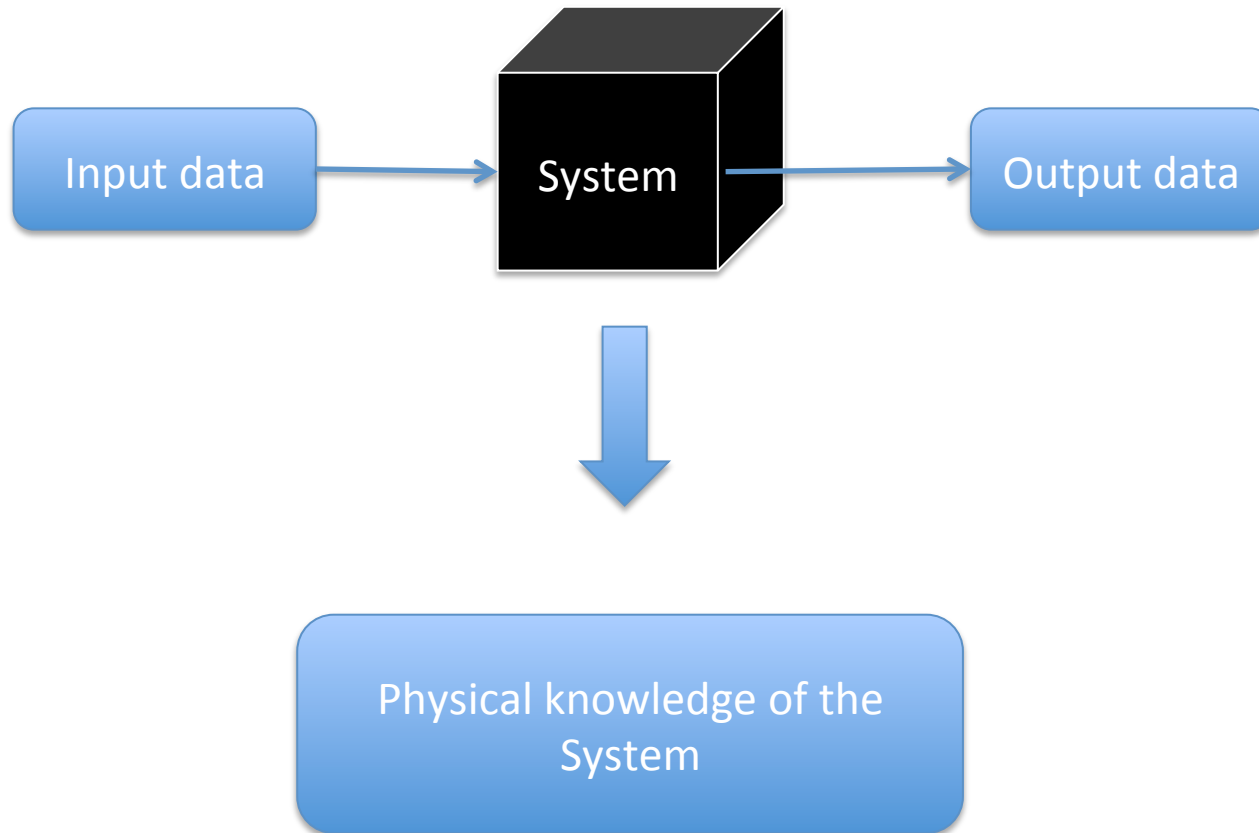


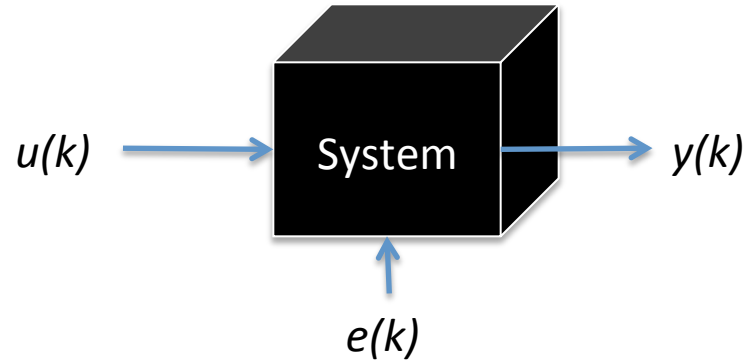
Required inputs

- Kp – measure of geomagnetic activity
- Boundary flux – characterise inflow of particles from magnetotail



Systems Approach





$$y(k) = F[y(k-1), \dots, y(k-n_y), \quad \text{System outputs}$$
$$u(k), \dots, u(k-n_u), \quad \text{System inputs}$$
$$e(k-1), \dots, e(k-n_e)] \quad \text{Noise/errors}$$

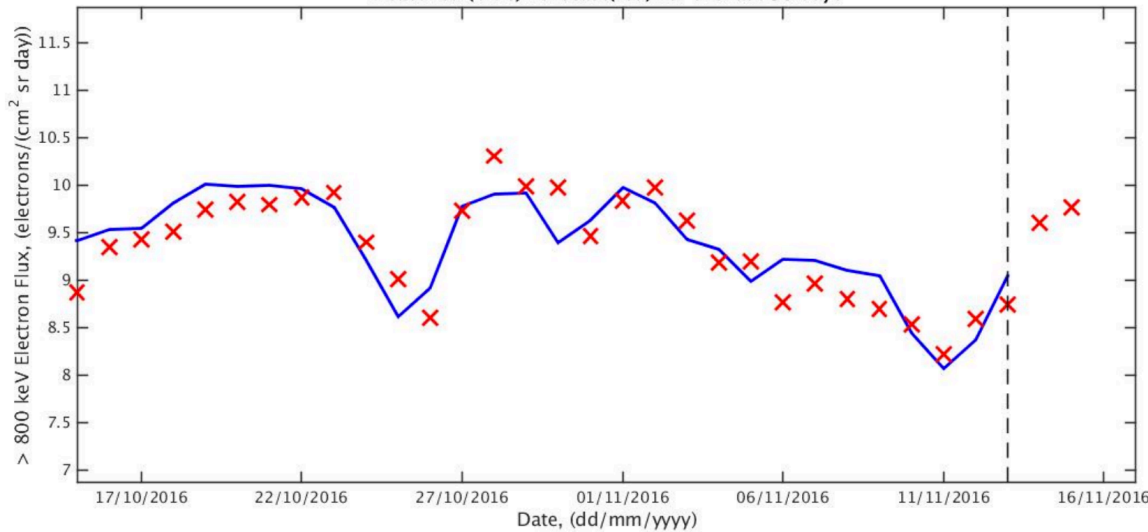
$F[]$ is a nonlinear function (polynomial, B-spline, radial basis function)

Three steps in NARMAX methodology

1. Structure selection
2. Coefficient estimation
3. Model validation

NARMAX

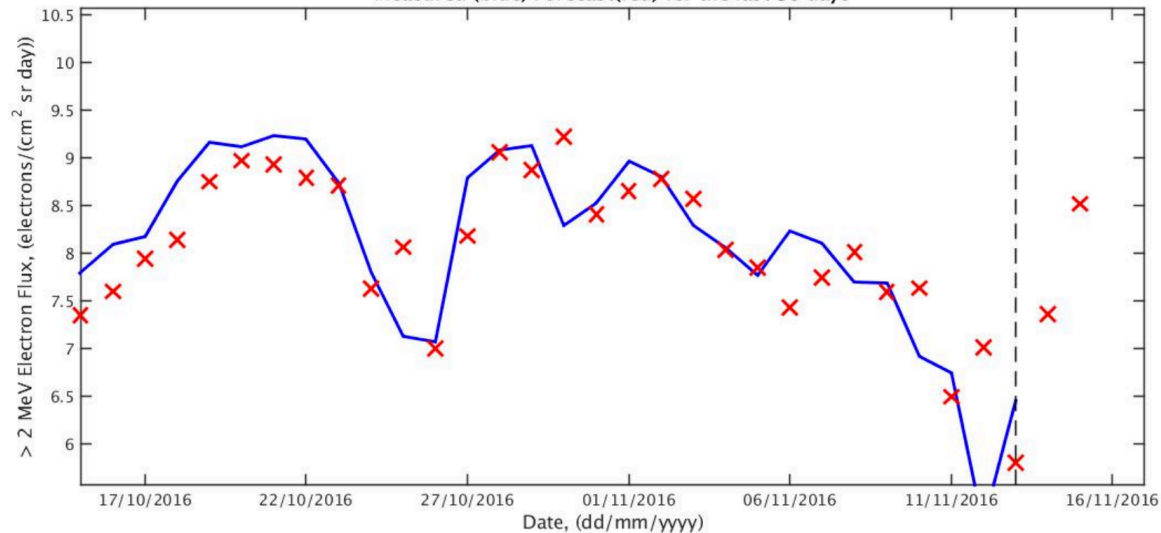
Daily Averaged Electron Flux at GEO
Measured (blue) Forecast (red) for the last 30 days



http://www.ssg.group.shef.ac.uk/USSW2/EF800k/800keV_EF.html

http://www.ssg.group.shef.ac.uk/USSW2/EF2M/2MeV_EF.html

Daily Averaged Electron Flux at GEO
Measured (blue) Forecast (red) for the last 30 days



First Principles

Require knowledge of all processes occurring within a system

Known/modeled processes may be included/excluded to determine their relative effects

Require drivers
Eg boundary electron fluxes,
Geomagnetic activity eg Kp or Dst

Calculate electron fluxes in wide range of L-shell

Lower accuracy

Systems Analysis

Often there is minimal knowledge of the system

All processes modeled as one system

Role of input parameters

Require constant stream of input data
Only usable at geostationary orbit

Limited to region of high data density
eg GSO

Resulting models are currently the most accurate

The VERB-NARMAX-Coupled model attempts to integrate these two different yet complementary approaches **for past/fore-casting** purposes.

NARMAX

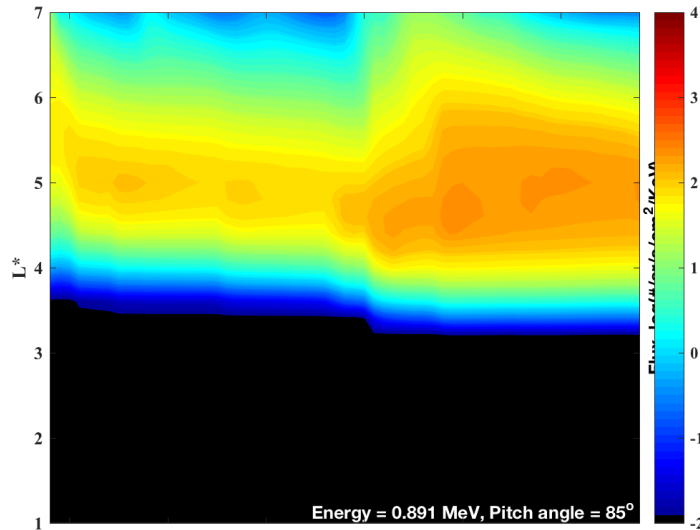
- Used to model measurements of electron fluxes at GEO based on data from GOES 13
- Provide a 24hr ahead forecast of electron fluxes at GEO

Model forecasts at GEO ($L^* \sim 6.2$) are used to estimate the outer boundary fluxes at $L^* = 7$ that are used by VERB

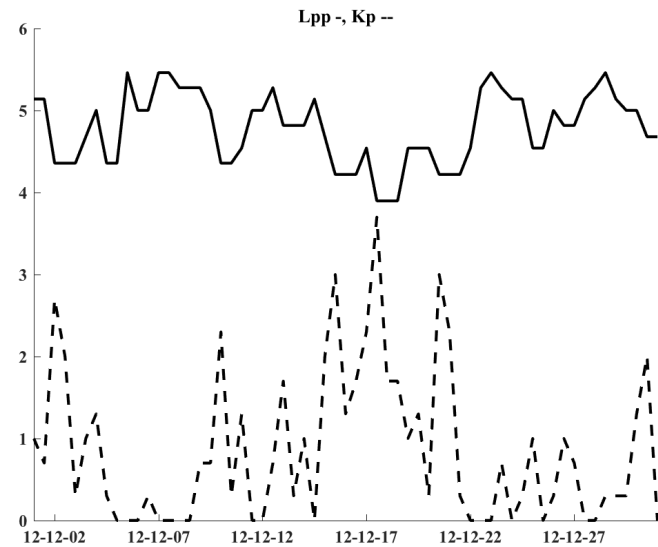
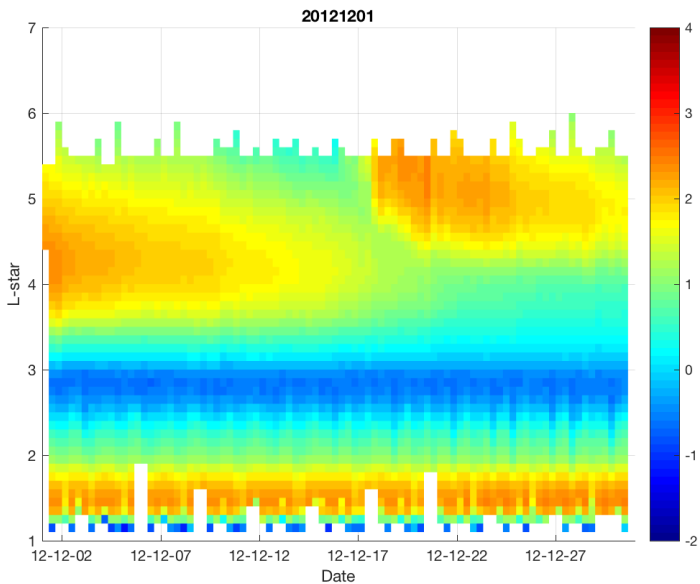
VERB

- Used to model the dynamics of the radiation belts based on estimated fluxes and K_p

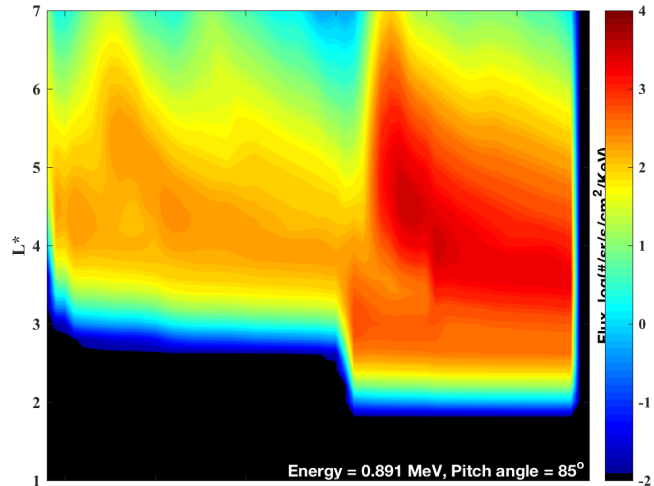
VNC Example 1



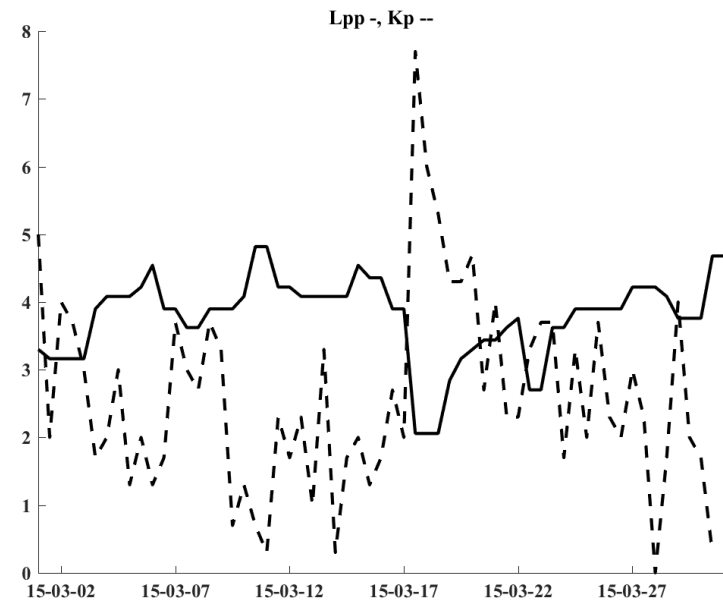
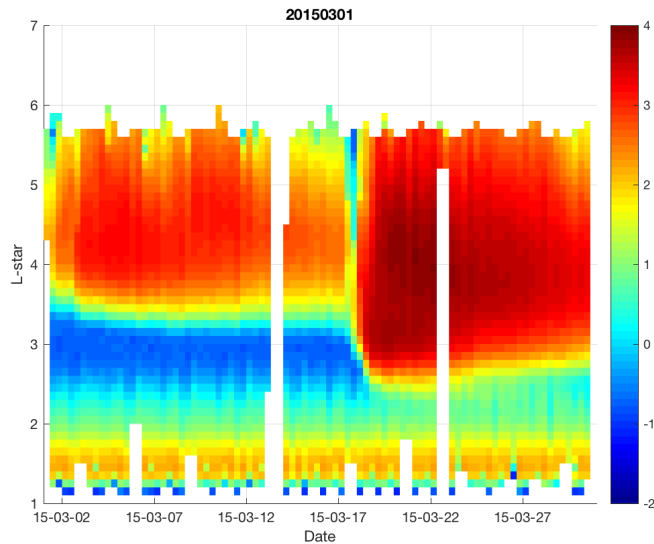
Quiet period



VNC Example 2



Disturbed period



Coupling of the VERB first principles and NARMAX systems models

- NARMAX was used to forecast daily fluxes of $>800\text{keV}$ and $>2\text{Mev}$ electrons at GEO
- These fluxes were used to estimate the input boundary fluxes required by VERB
- VERB was then used to simulate the electron fluxes
- Qualitatively, the results reproduce measurements from the Van Allen Probes MagEIS instrument

Under development

- Current (preliminary) Kp values from GFZ, Potsdam
- Forecasts of Kp
 - Wing model
 - Sheffield, Lund (EU funded project **PROGRESS**)
- Quantitative comparison with experimental data

Future plans

- Transfer system to web server
- Access <https://ssg.group.shef.ac.uk/progress/html/>



This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 637302