



PROGRESS Final Review Meeting  
2-3 August 2018  
Sheffield



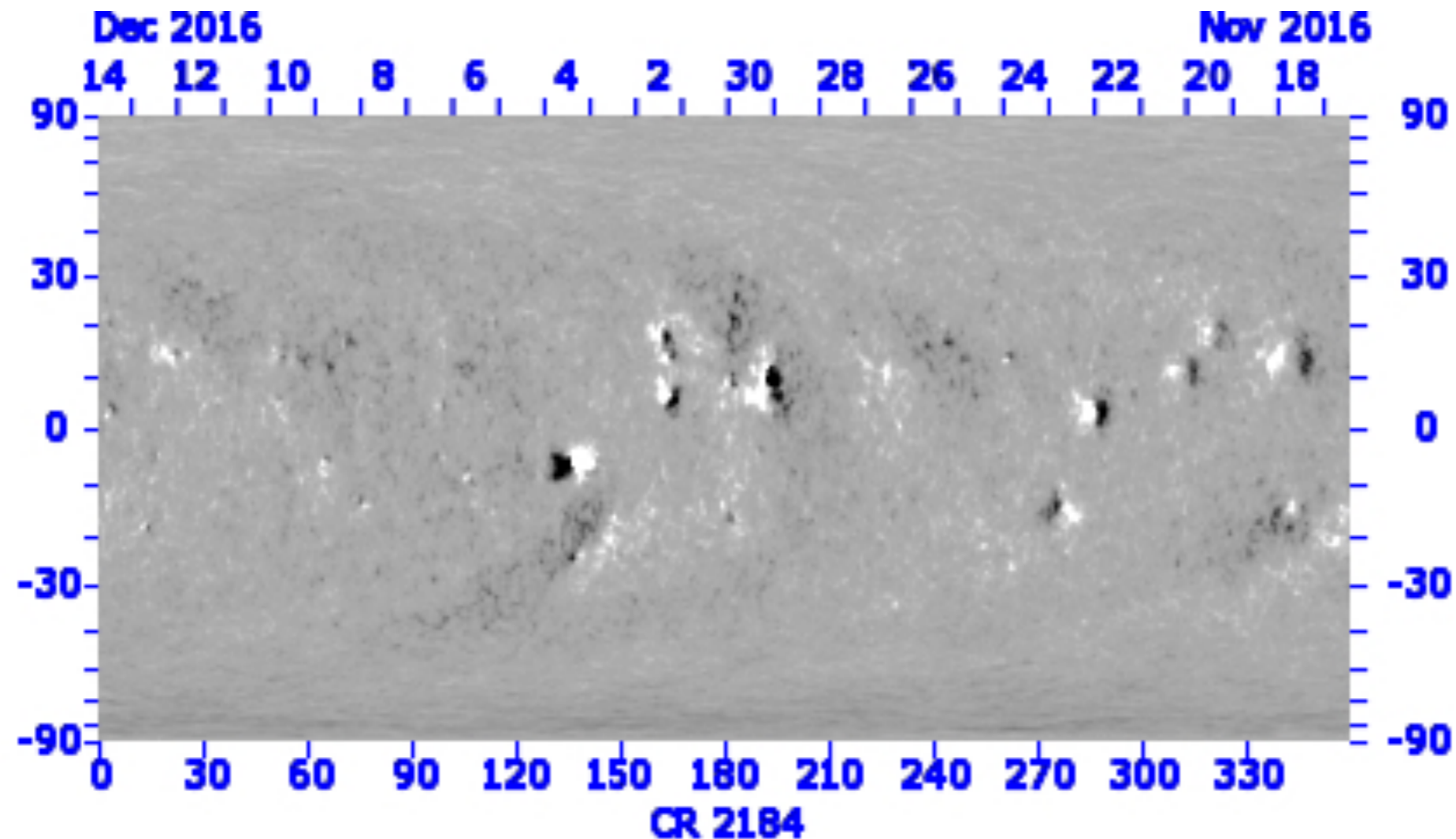
## WP 2 - Propagation of the solar wind from the Sun to L1

**Tony Arber**, Warwick  
Keith Bennett, Warwick  
Bart van der Holst, Michigan  
Mike Liemohn, Michigan



# Objective

From solar surface predict the MHD variables at L1 and 1 A.U.  
using **first principles physics** models

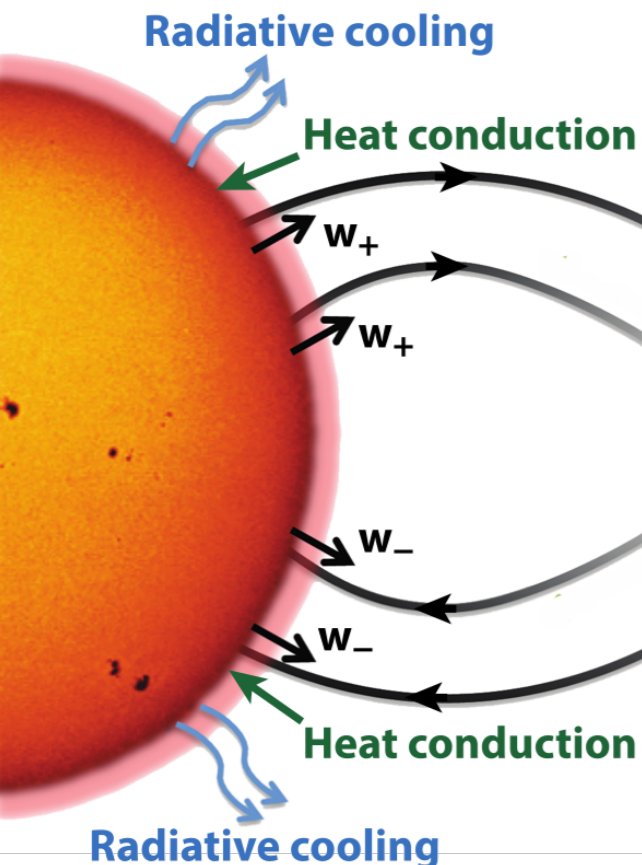


# Multi-layered coupled modelling

GONG data used to get potential B-field

Use potential field as starting point for **AWSoM** simulation

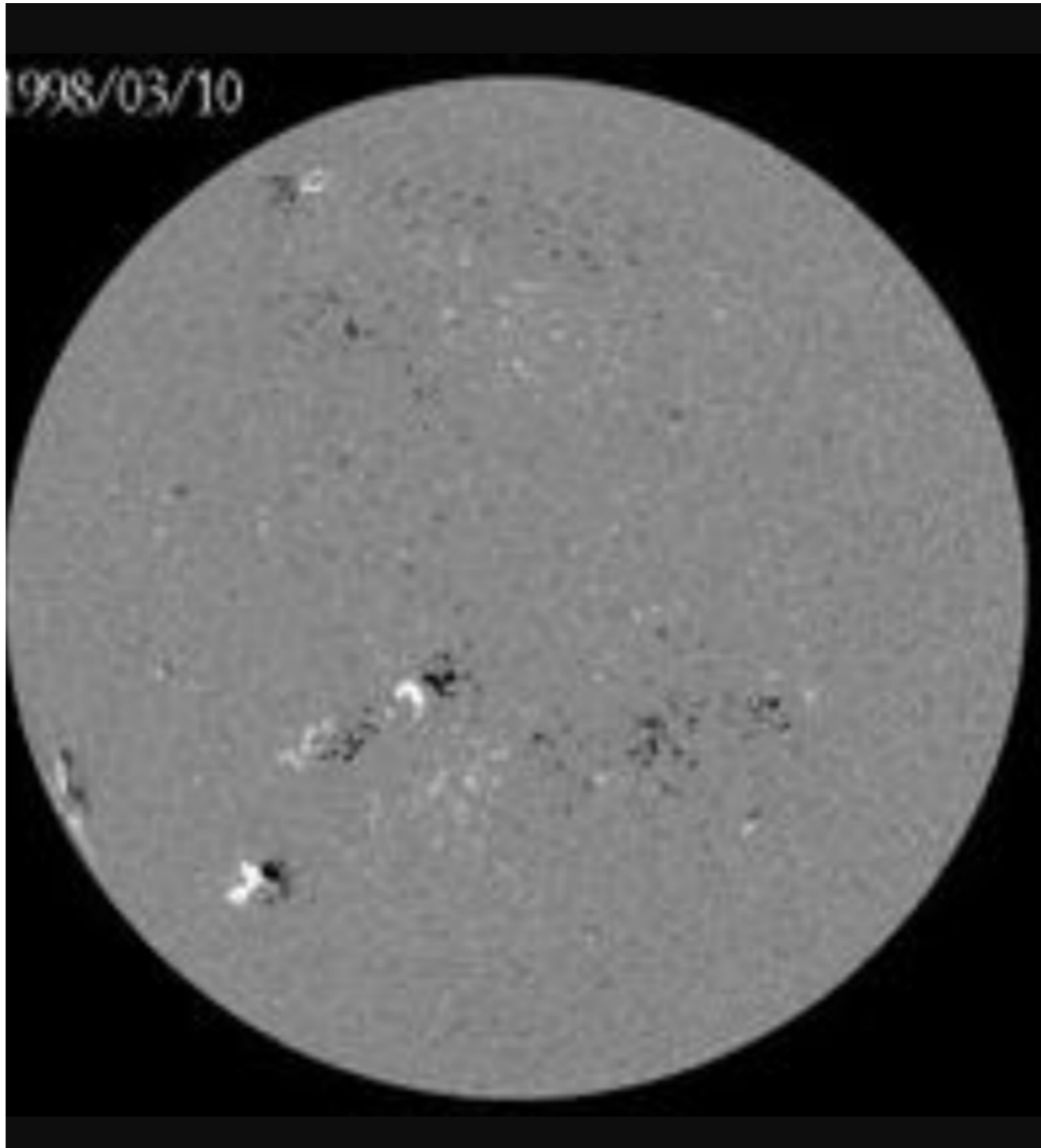
At 20 Solar radii data interpolated from AWSoM onto **SWIFT** grid and solution propagated to 1 AU



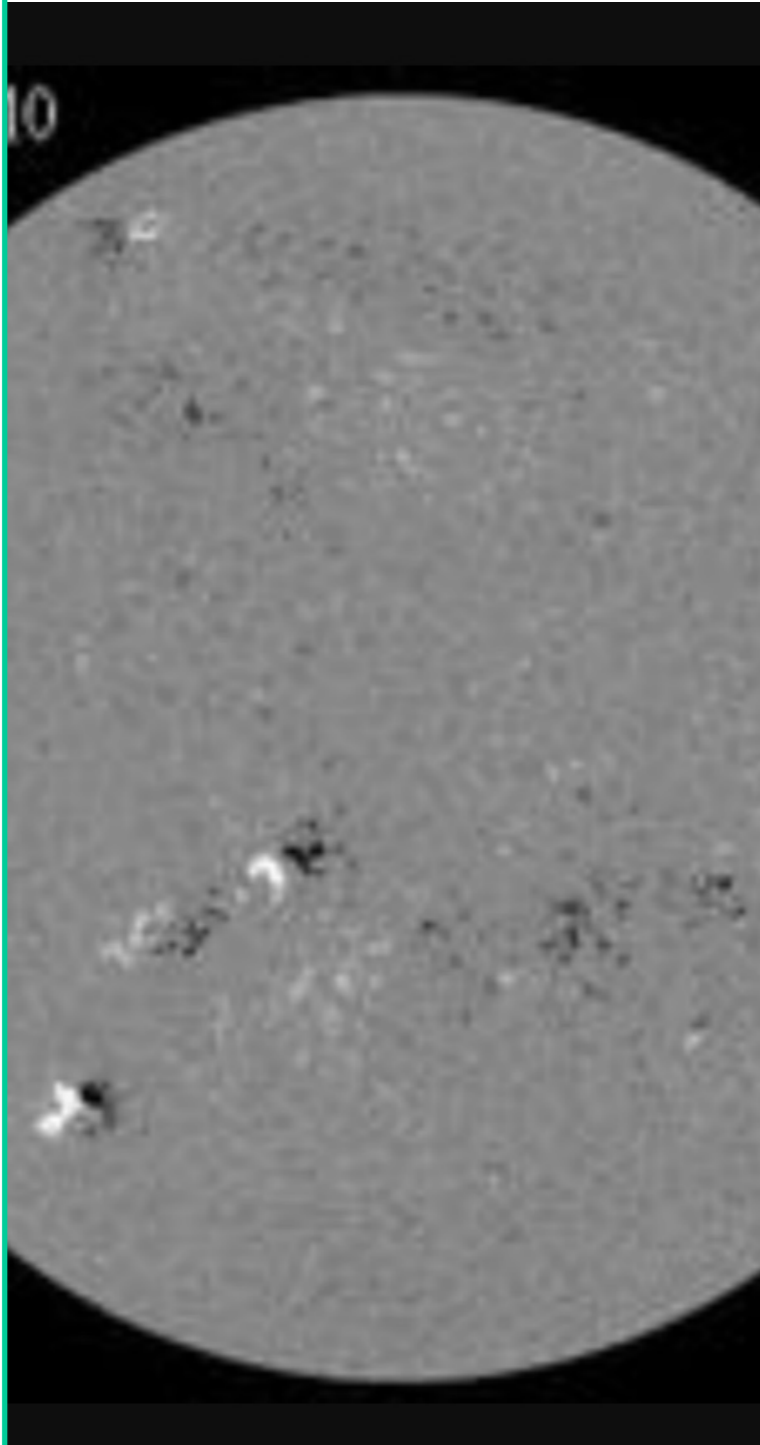
AWSoM used to replace the WSA in WSA-ENLIL with a first principles physics package

SWIFT should be viewed as essential an EU variant of the widely used ENLIL code

# GONG data disk image

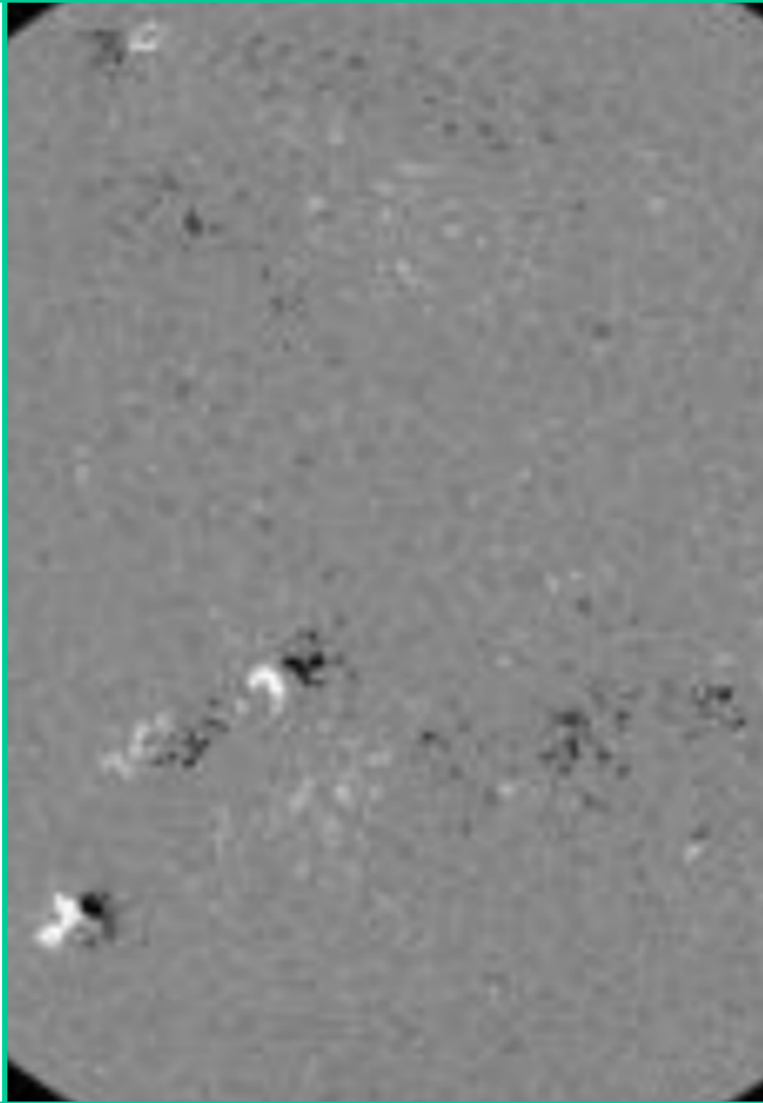


# GONG data disk image



Line-of-sight so only  
120 degrees used

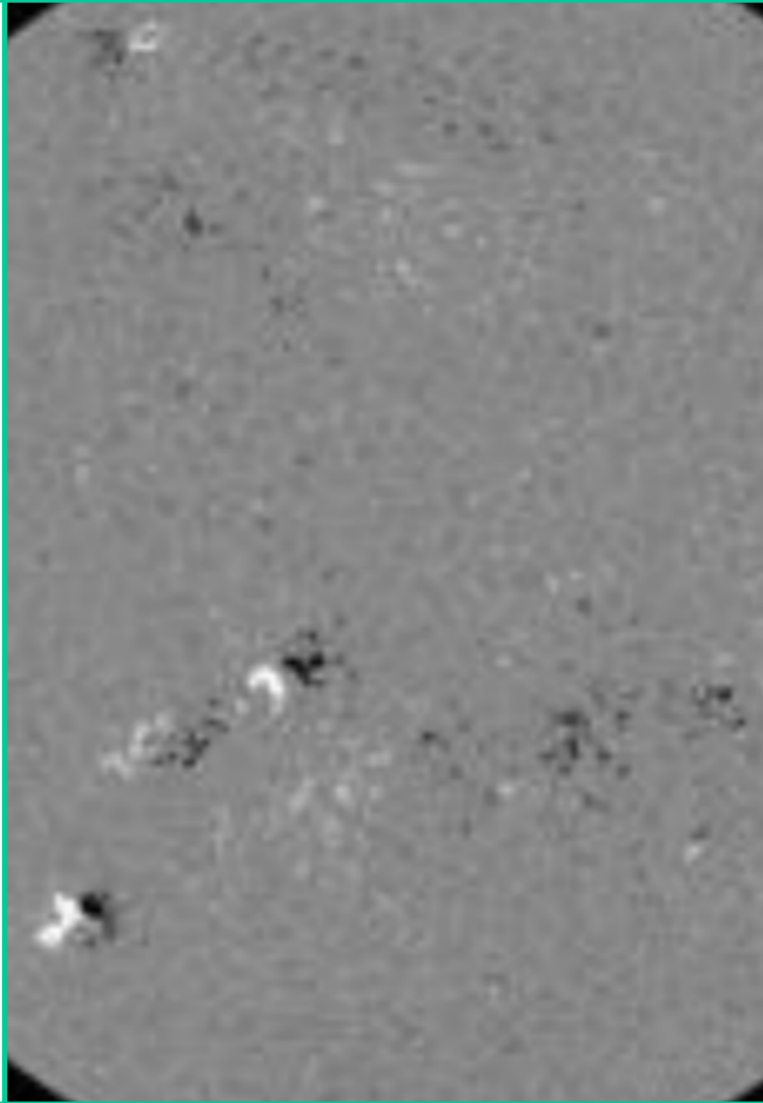
# GONG data disk image



Line-of-sight so only  
120 degrees used

Poor resolution at poles so  
fitting schemes needed

# GONG data disk image



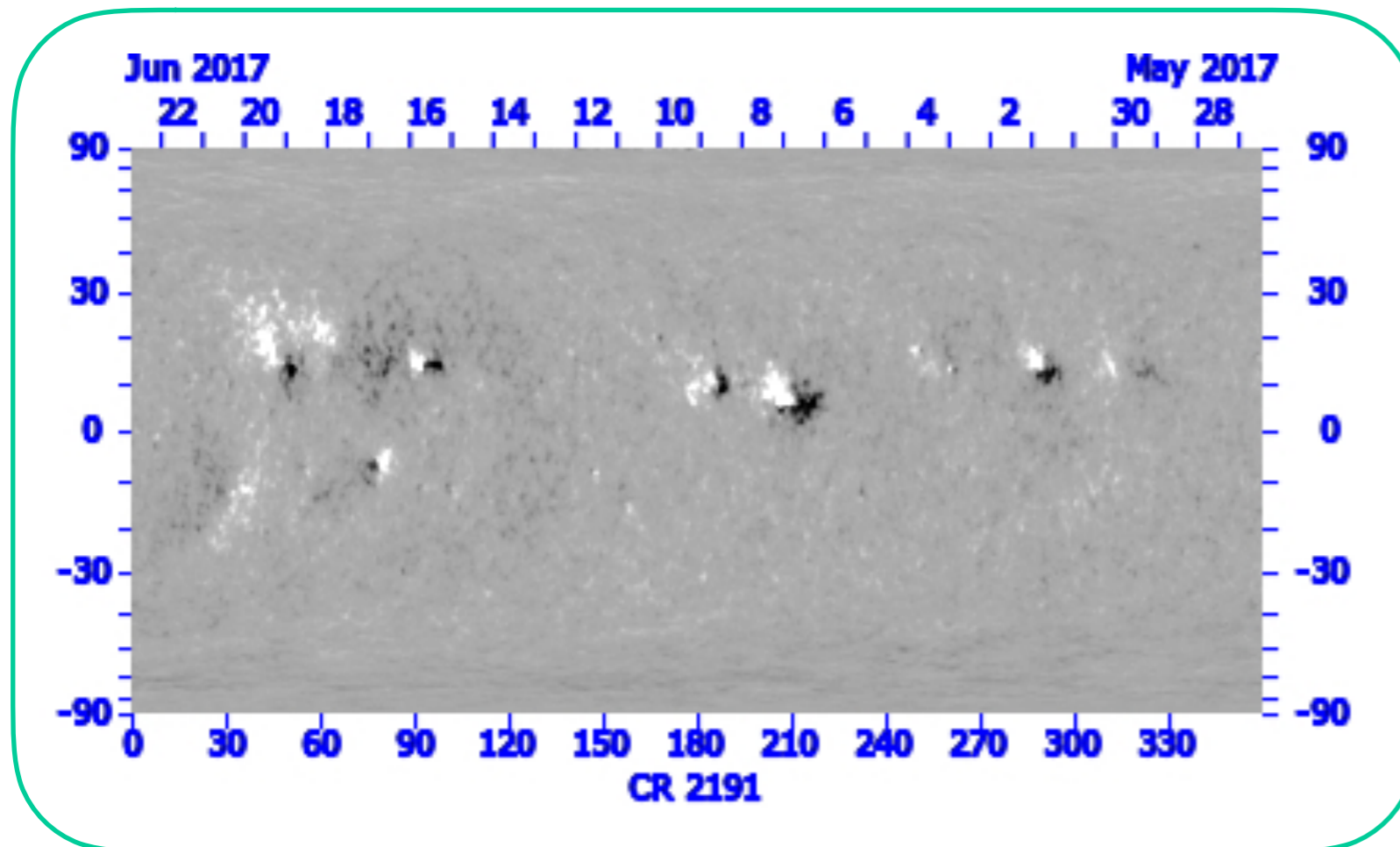
Line-of-sight so only  
120 degrees used

Poor resolution at poles so  
fitting schemes needed

Project onto  
longitude-latitude

# GONG Data

6 GONG sites take full-disk images every ~minute



These are averaged into 10 minute images

Image covers 120 degrees

Overlapping images averaged with a weight based on  $\cos^4(\phi)$

A full rotation image can be updated every ~8hrs

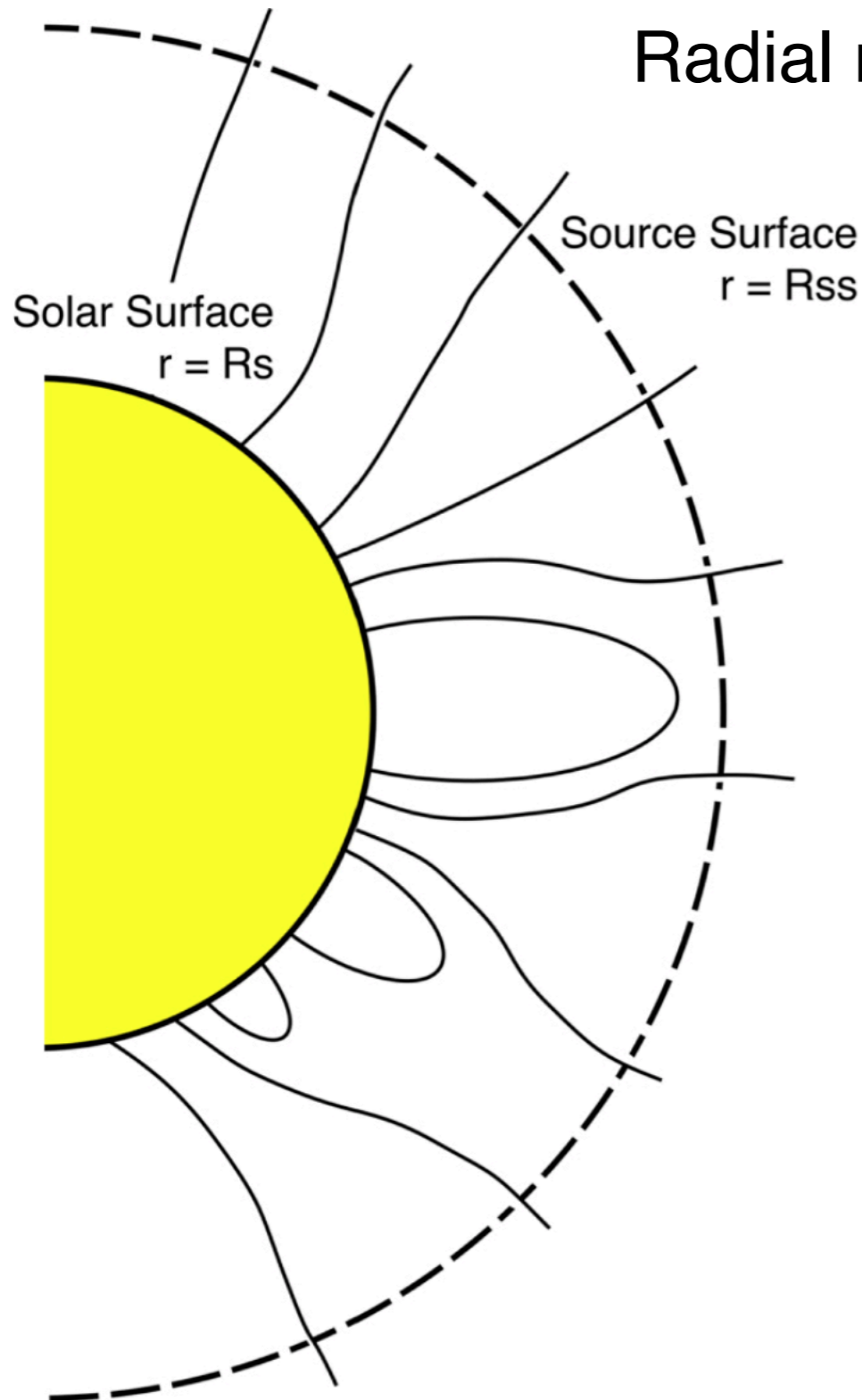
Hourly updates need special treatment of western edge weighting

Poles are poorly resolved and need extrapolation...



# Potential Field Source Surface (PFSS)

Radial magnetic field at the solar surface from GONG



Chose a surface  $R_{ss}$ , usually at  $2.5 R_{sun}$

On  $R_{ss}$  fix the field to be radial to match field structure expected due to solar wind

Potential field between  $R_{sun}$  and  $R_{ss}$

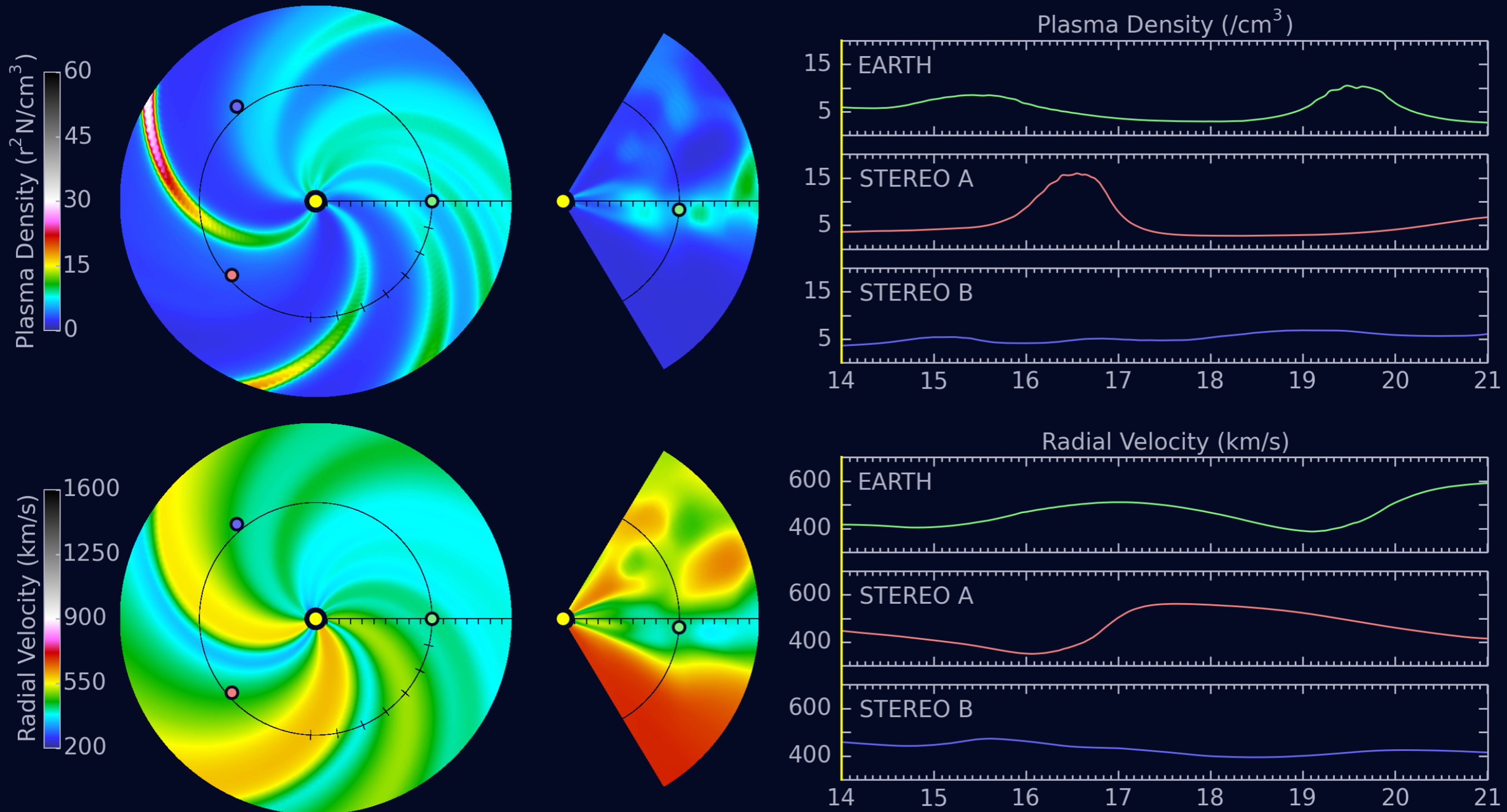
$$\mathbf{B} = -\nabla\Phi$$

$$\mathbf{j} = \nabla \times \mathbf{B} = 0$$

$$\nabla^2\Phi = 0$$

# WSA-ENLIL typical results

2017-05-14 00:00:00



# PROGRESS Project

Aim to predict MHD variables at 1 A.U. from GONG data

Replace empirical models of WSA with first principles model

Allow full vector B-field

Use 2 temperature MHD

Shock heating of ions, thermal conduction in electrons

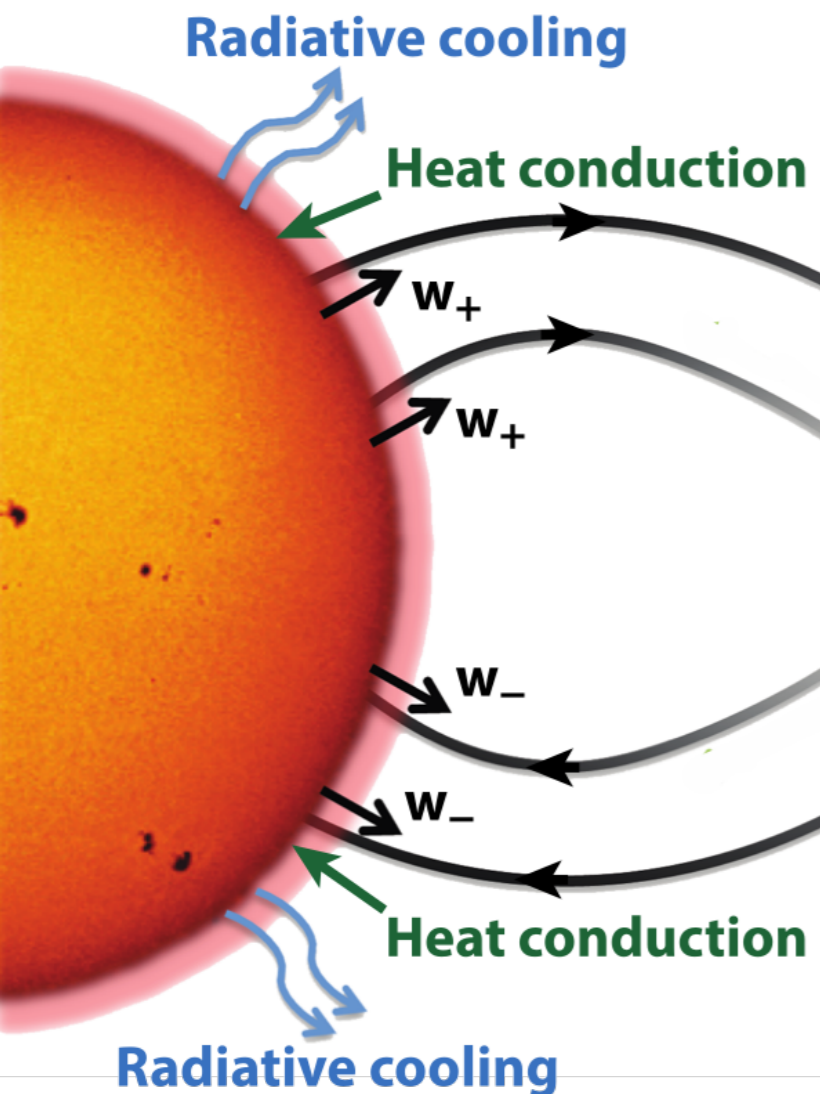
# Alfvén Wave Solar Model (AWSoM)



B. van der Holst et al. ApJ 782, 81 (2014).

## Extended MHD physics:

- Two ( $T_i, T_e$ ) or three ( $T_{i\parallel}, T_{i\perp}, T_e$ ) temperatures
- Equations for parallel and antiparallel propagating turbulence ( $w_{\pm}$ )
- Physics-based reflection of  $w_{\pm}$  results in turbulent cascade
- Physics-based apportioning of turbulence dissipation (at the gyro-radius scales) into coronal heating of various species
- Wave pressure gradient acceleration of solar wind plasma
- Collisional and collisionless electron heat conduction
- Radiative plasma cooling using CHIANTI



Solves for the Alfvén wave energy, across all wave-numbers, propagating along **B** and against **B**.

# Mathematical Models

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0,$$

$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{u} \mathbf{B} - \mathbf{B} \mathbf{u}) = 0,$$

$$\frac{\partial(\rho \mathbf{u})}{\partial t} + \nabla \cdot \left( \rho \mathbf{u} \mathbf{u} - \frac{\mathbf{B} \mathbf{B}}{\mu_0} \right) + \nabla \left( P_i + P_e + \frac{B^2}{2\mu_0} + P_A \right) = -\frac{GM_{\odot} \rho \mathbf{R}}{R^3},$$

Normal MHD + 2T and Alfvén pressure

$$P_A = \frac{1}{2} (w_+ + w_-)$$

# Mathematical Models

$$\frac{\partial}{\partial t} \left( \frac{P}{\gamma - 1} + \frac{\rho u^2}{2} + \frac{\mathbf{B}^2}{2\mu_0} \right) + \nabla \cdot \left\{ \left( \frac{\rho u^2}{2} + \frac{\gamma P}{\gamma - 1} + \frac{B^2}{\mu_0} \right) \mathbf{u} - \frac{\mathbf{B}(\mathbf{u} \cdot \mathbf{B})}{\mu_0} \right\} =$$
$$= -(\mathbf{u} \cdot \nabla) P_A + \nabla \cdot (\kappa \cdot \nabla T) - Q_{\text{rad}} + \Gamma_- w_- + \Gamma_+ w_+ - \frac{GM_{\odot} \rho \mathbf{r} \cdot \mathbf{u}}{r^3},$$

Heating from Alfvén wave turbulence

$$\Gamma_{\pm} = \frac{2}{L_{\perp}} \sqrt{\frac{w_{\mp}}{\rho}}$$

$$\frac{\partial w_{\pm}}{\partial t} + \nabla \cdot [(\mathbf{u} \pm \mathbf{V}_A)w_{\pm}] + \frac{w_{\pm}}{2}(\nabla \cdot \mathbf{u}) = \mp \mathcal{R} \sqrt{w_- w_+} - \Gamma_{\pm} w_{\pm}$$

Turbulence energy advection and reflection

$$\mathcal{R} = \min \left\{ \sqrt{(\mathbf{b} \cdot [\nabla \times \mathbf{u}])^2 + [(\mathbf{V}_A \cdot \nabla) \log V_A]^2}, \max(\Gamma_{\pm}) \right\} \times \\ \times \left[ \max \left( 1 - \frac{I_{\max}}{\sqrt{w_+/w_-}}, 0 \right) - \max \left( 1 - \frac{I_{\max}}{\sqrt{w_-/w_+}}, 0 \right) \right],$$

- Wave energy densities of counter-propagating transverse Alfvén waves parallel (+) and anti-parallel (-) to magnetic field:

energy reduction in expanding flow

$$\frac{\partial w_{\pm}}{\partial t} + \nabla \cdot [(\mathbf{u} \pm \mathbf{V}_A)w_{\pm}] + \frac{w_{\pm}}{2}(\nabla \cdot \mathbf{u}) = \mp \mathcal{R}\sqrt{w_-w_+} - \Gamma_{\pm}w_{\pm}$$

↑  
Alfvén wave advection
↑  
wave reflection

↓  
wave dissipation

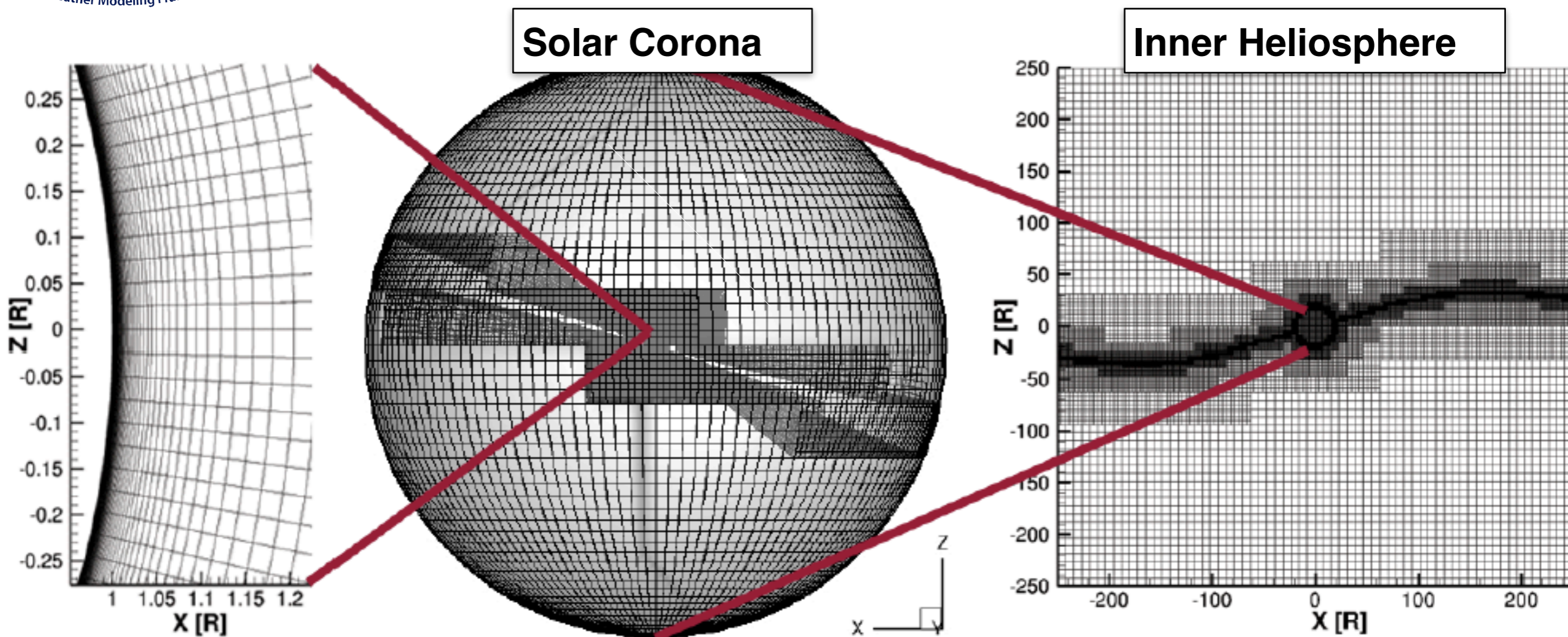
- The wave reflection is due to field-aligned component of the Alfvén speed gradient and vorticity.

- Phenomenological wave dissipation (Dmitruk et al., 2002):  $\Gamma_{\pm} = \frac{2}{L_{\perp}} \sqrt{\frac{w_{\mp}}{\rho}}$
- Similar to Hollweg (1986), we use a simple scaling law for the transverse correlation length  $L_{\perp} \sqrt{B} = 150 \text{ km} \sqrt{T}$

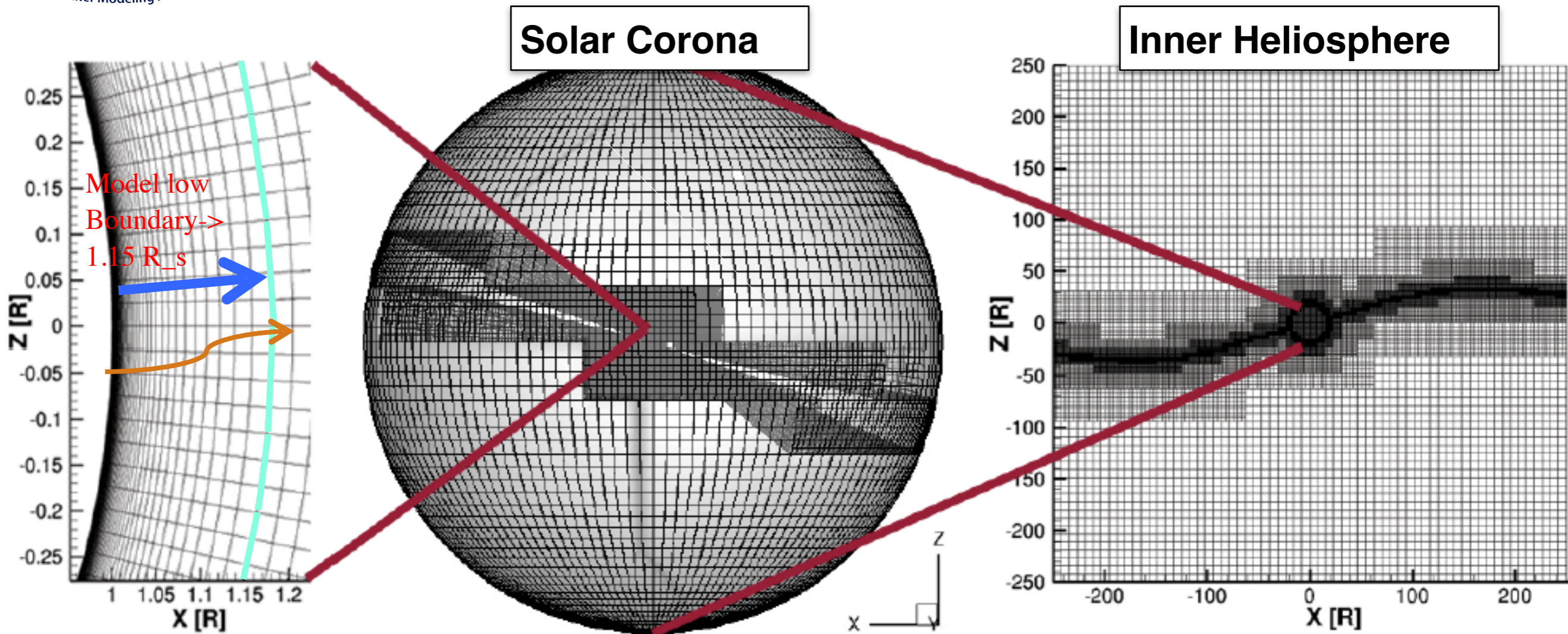
- Poynting flux of outward propagating turbulence:  $(S_A/B)_{\odot} = 1.1 \times 10^6 \text{ W m}^{-2} \text{ T}^{-1}$



# Computational Grid: AWSoM

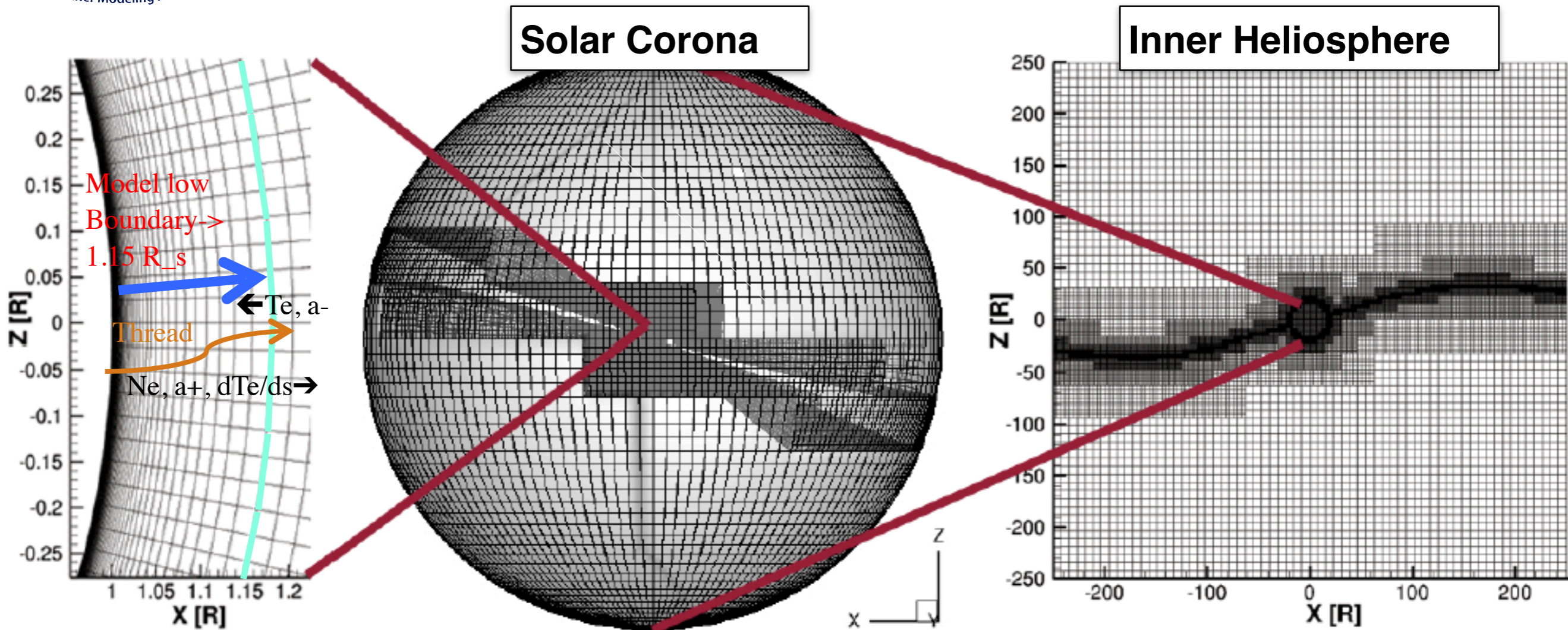


- AWSoM uses stretched spherical grid for solar corona
- Significant grid stretching to grid resolve the upper chromosphere and transition region in addition to artificial transition region broadening
- Due to the very high resolution below  $1.15R_{\text{sun}}$  AWSoM is too slow to achieve faster than real-time.



- We use the lower boundary of the AWSoM-R model at  $R = 1.15R_s$
- We apply 1D thread solutions along PFSS model field lines to bridge the AWSoM-R model to the chromosphere through the transition region.

# Apply 1D Thread Solution



- Recognise that between  $1R_s$  and  $1.15R_s$   $u \parallel B$  and  $u \ll v_{MHD}$
- Quasi-steady-state mass, momentum, energy transport and wave turbulence transport is solved along the connecting field line implicitly (**1D** equations!)
- The speed-up of AWSoM-R is about a factor 200 compared to AWSoM

**Still takes 14 hrs on 128 cores to run from one GONG map**

# AWSoM - SWIFT Coupling

AWSoM provides MHD variable at  $21.5 R_{sun}$

AWSoM is in co-rotating frame but output to buffer in inertial

SWIFT uses the inertial frame buffer MHD values as driver for 2T MHD solution of

$$\begin{aligned}\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) &= 0, \\ \frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{u} \mathbf{B} - \mathbf{B} \mathbf{u}) &= 0, \\ \frac{\partial (\rho \mathbf{u})}{\partial t} + \nabla \cdot \left( \rho \mathbf{u} \mathbf{u} - \frac{\mathbf{B} \mathbf{B}}{\mu_0} \right) + \nabla \cdot \left( P_i + P_e + \frac{B^2}{2\mu_0} + P_A \right) &= -\frac{GM_{\odot} \rho \mathbf{R}}{R^3},\end{aligned}$$

Energy equations for each species

$$\frac{\partial}{\partial t} \left( \frac{P}{\gamma - 1} \right) + \nabla \cdot \left( \frac{P}{\gamma - 1} \mathbf{u} \right) + P \nabla \cdot \mathbf{u} = -\nabla \cdot \mathbf{q}_e + H_{shock}$$

Shock heating of ions, thermal conduction for electrons

# SWIFT Thermal Conduction

Electron mean-free-path in SW is roughly 1 A.U.

Classical Spitzer-Harm conduction not valid

Instead adopt approach of Hollweg

Maximum heat carried by electrons  $\mathbf{q}_e = \alpha P_e \mathbf{u}_e$

$$\frac{\partial}{\partial t} \left( \frac{P_e}{\gamma - 1} \right) + \nabla \cdot \left( \frac{P_e}{\gamma_c - 1} \mathbf{u} \right) + P_e \nabla \cdot \mathbf{u} = 0$$

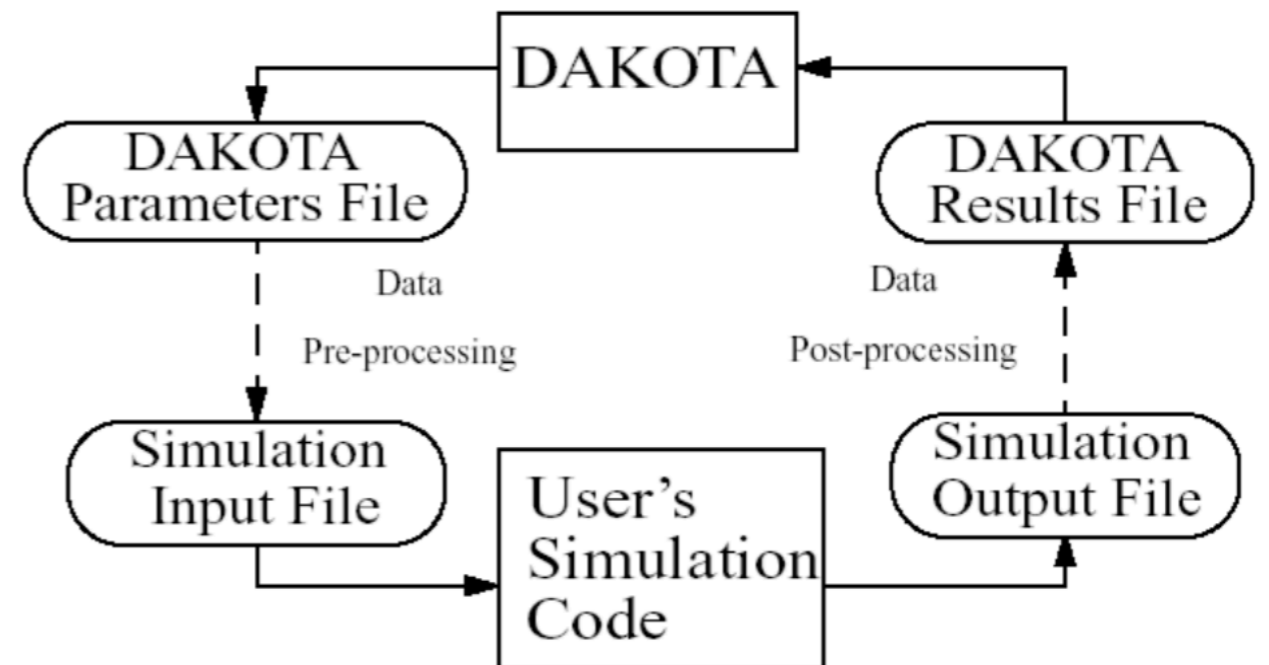
With 
$$\gamma_c = \frac{\gamma + (\gamma - 1)\alpha}{1 + (\gamma - 1)\alpha}$$

No satisfactory solution to parallel conduction fast enough for a prediction code

The Dakota toolkit provides an interface between simulation codes and iterative analysis methods.[2]

Contains algorithms for optimization, uncertainty quantification (UQ), parameter studies, calibration, and sensitivity/variance analysis.

We perform a Sensitivity Analysis (SA) of AWSoM/SWIFT on the three free parameters, quantifying accuracy of solar wind predictions using the  $L_1$ -norm compared to OMNI data.



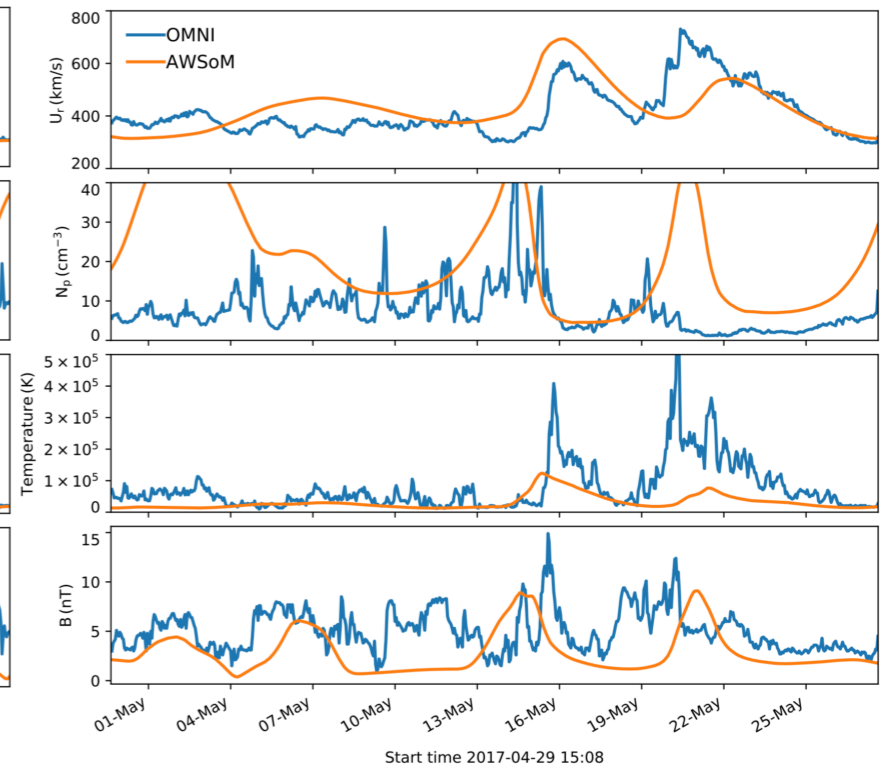
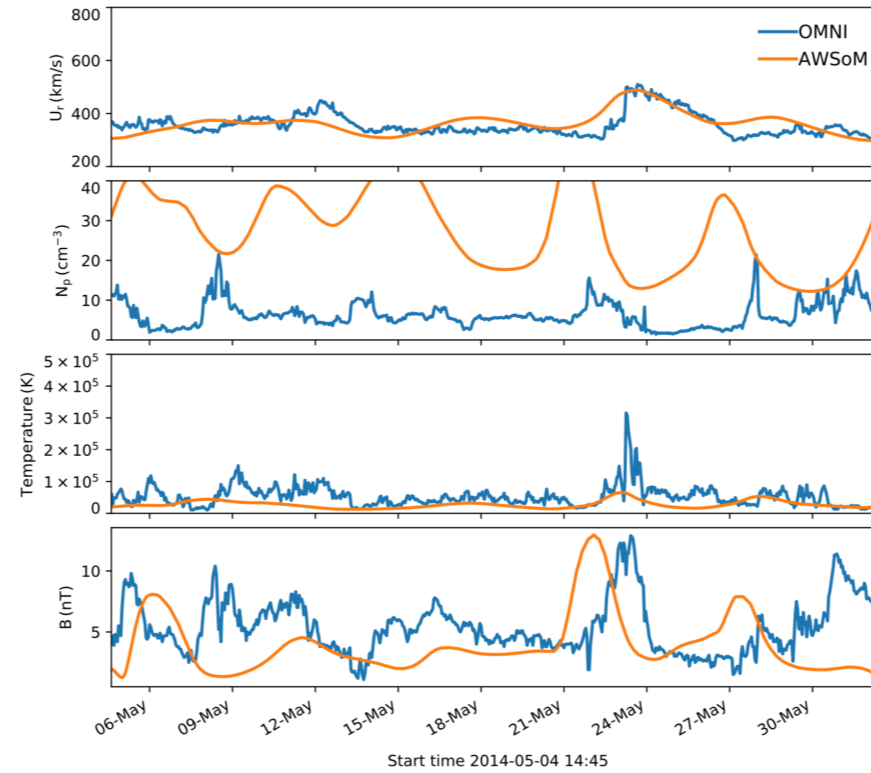
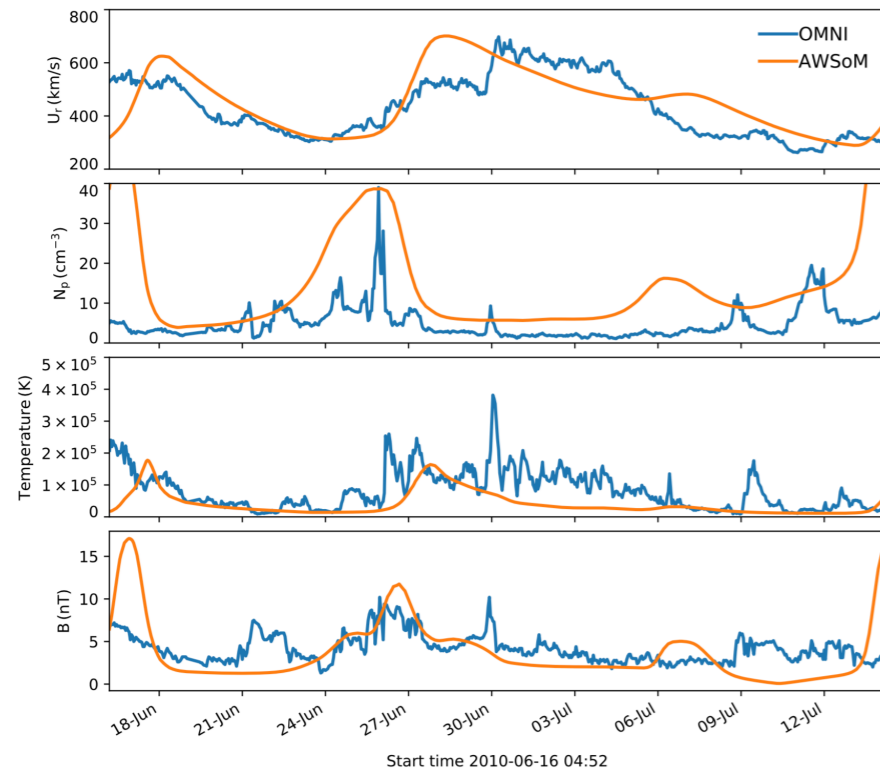
$$\|L_i\| = \left\{ \frac{1}{n} \sum^n [\mathbf{u}_{sim} - \mathbf{u}_{OMNI}]^i \right\}^{\frac{1}{i}}$$

# Best fit $L1$ results for three Carrington rotations

June 2010

May 2014

May 2017



$$(S_A/B)_{\cdot} = 0.9 \times 10^6 \text{Wm}^{-2} \text{T}^{-1}$$

$$(S_A/B)_{\cdot} = 1.1 \times 10^6 \text{Wm}^{-2} \text{T}^{-1}$$

$$(S_A/B)_{\cdot} = 1.5 \times 10^6 \text{Wm}^{-2} \text{T}^{-1}$$

The best reliable fit was selected as:

Poynting flux per unit B =  $1.1 \text{e}6 \text{ Wm}^{-2} \text{ T}^{-1}$

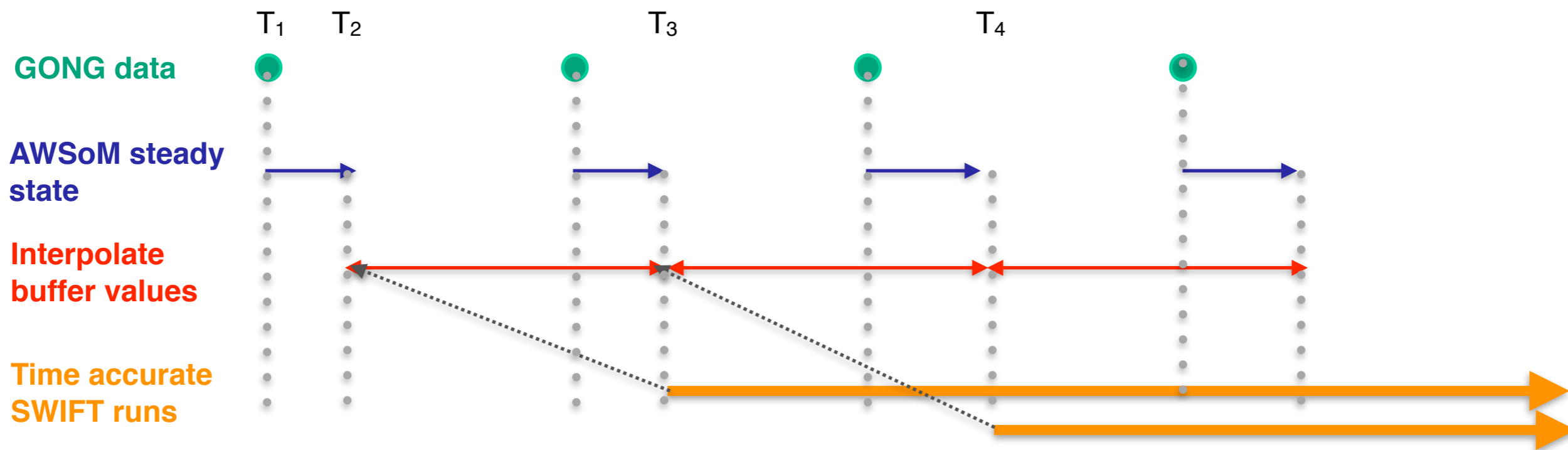
Stochastic exponent (controls Alfvén wave heating) = 0.34

While scaling GONG can improve fit this was not chosen as no physics reason to justify

Allowed us to reduce runtime to 14 hours on 32 cores so fits on a workstation

# AWSoM-SWIFT Time Dependent

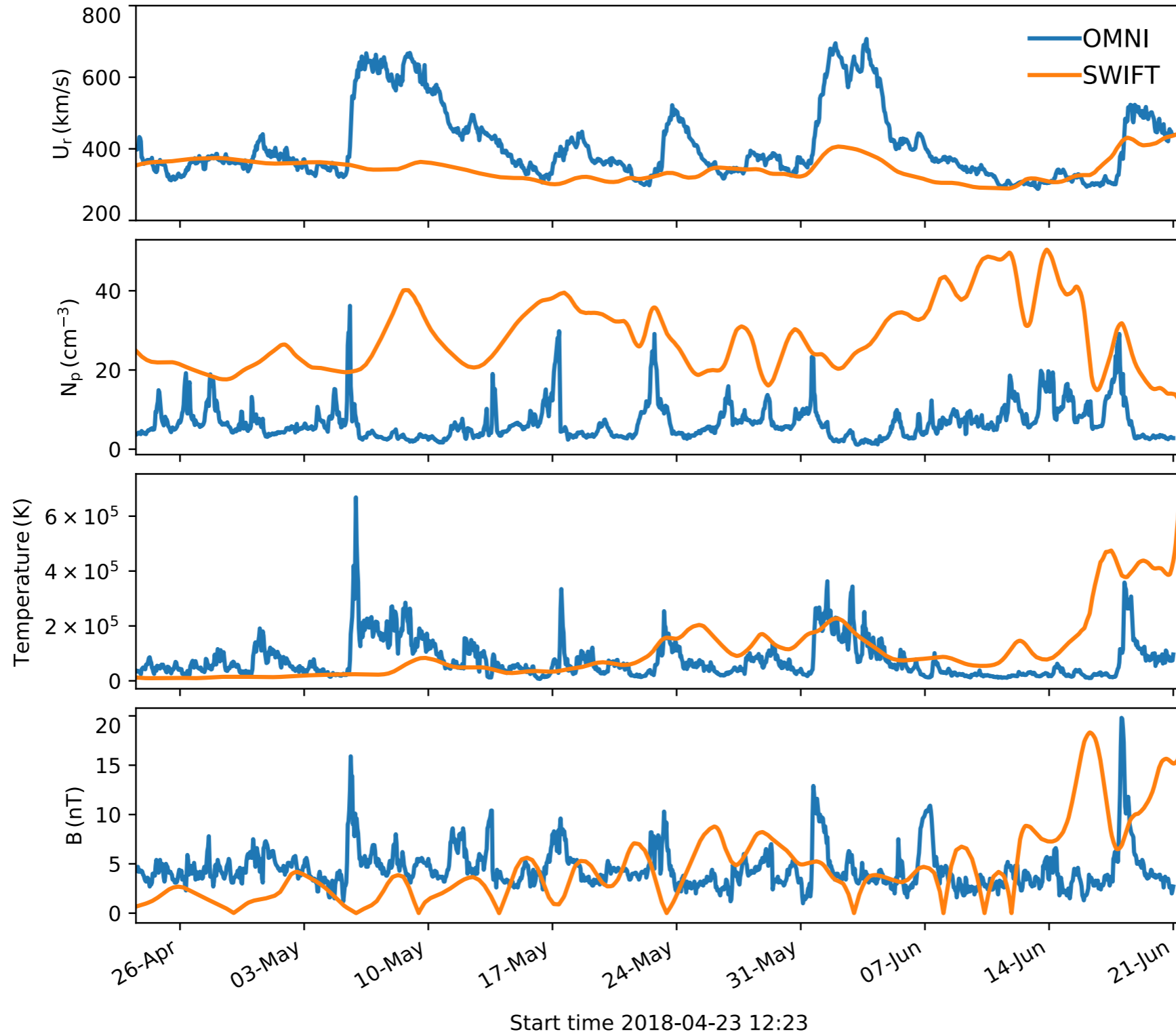
Time accurate for comparison with OMNI and WSA-ENLIL

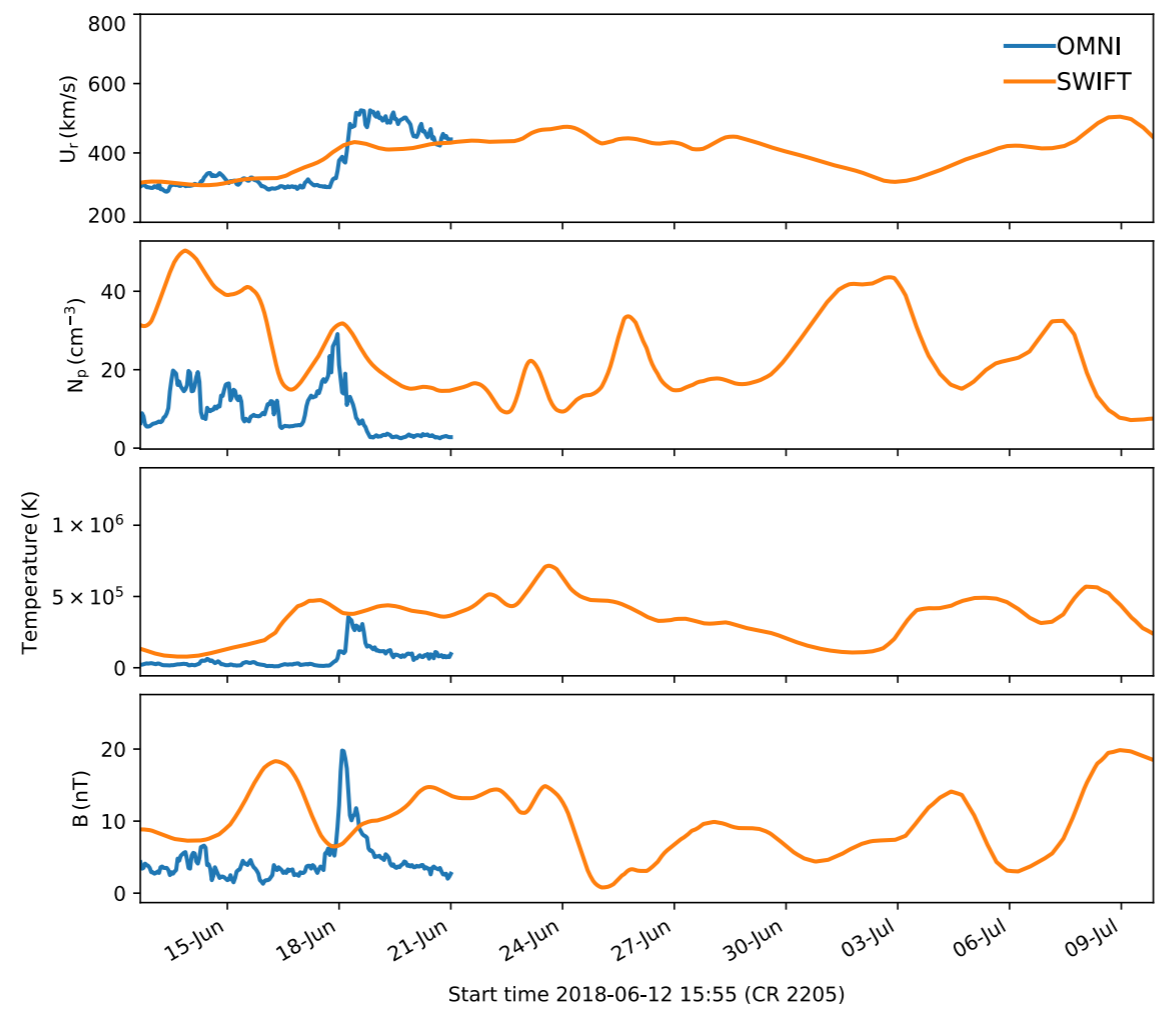
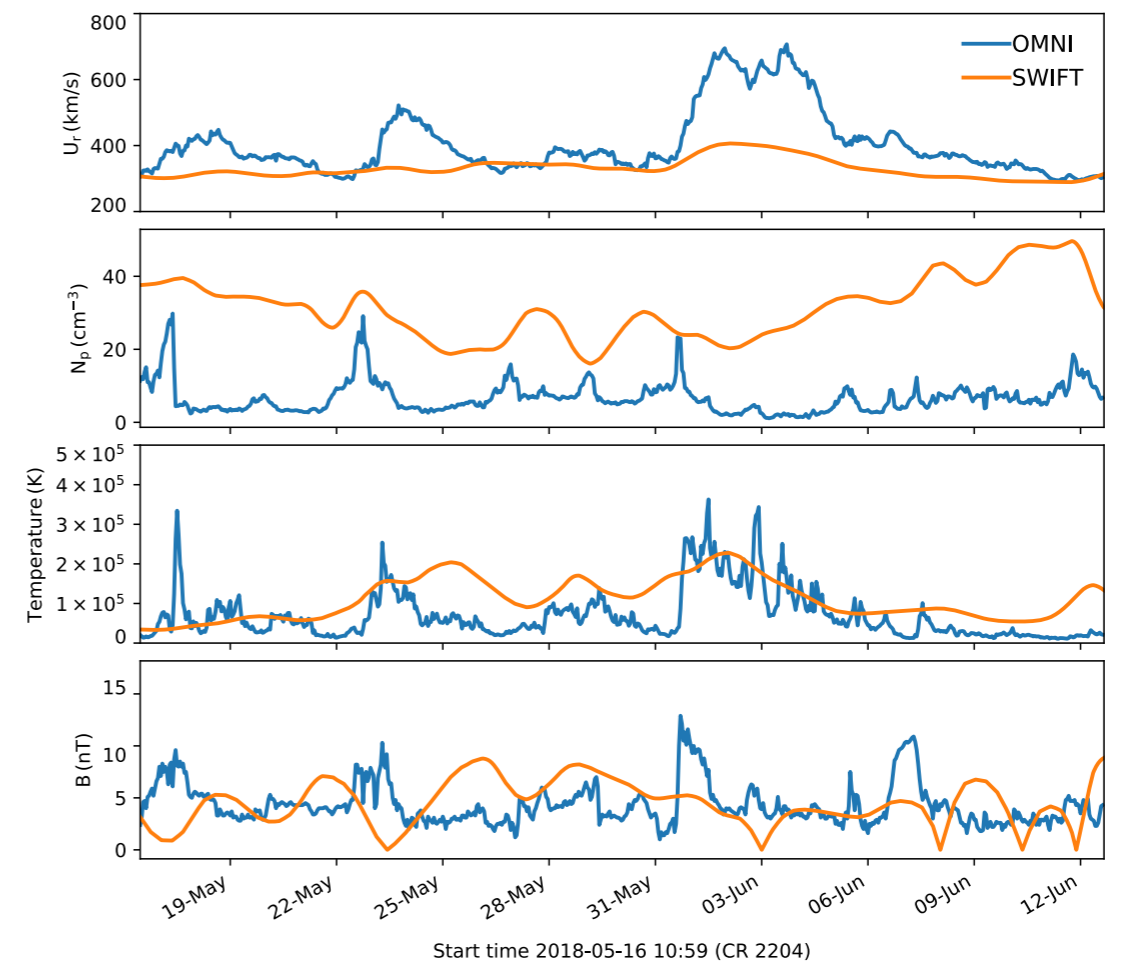
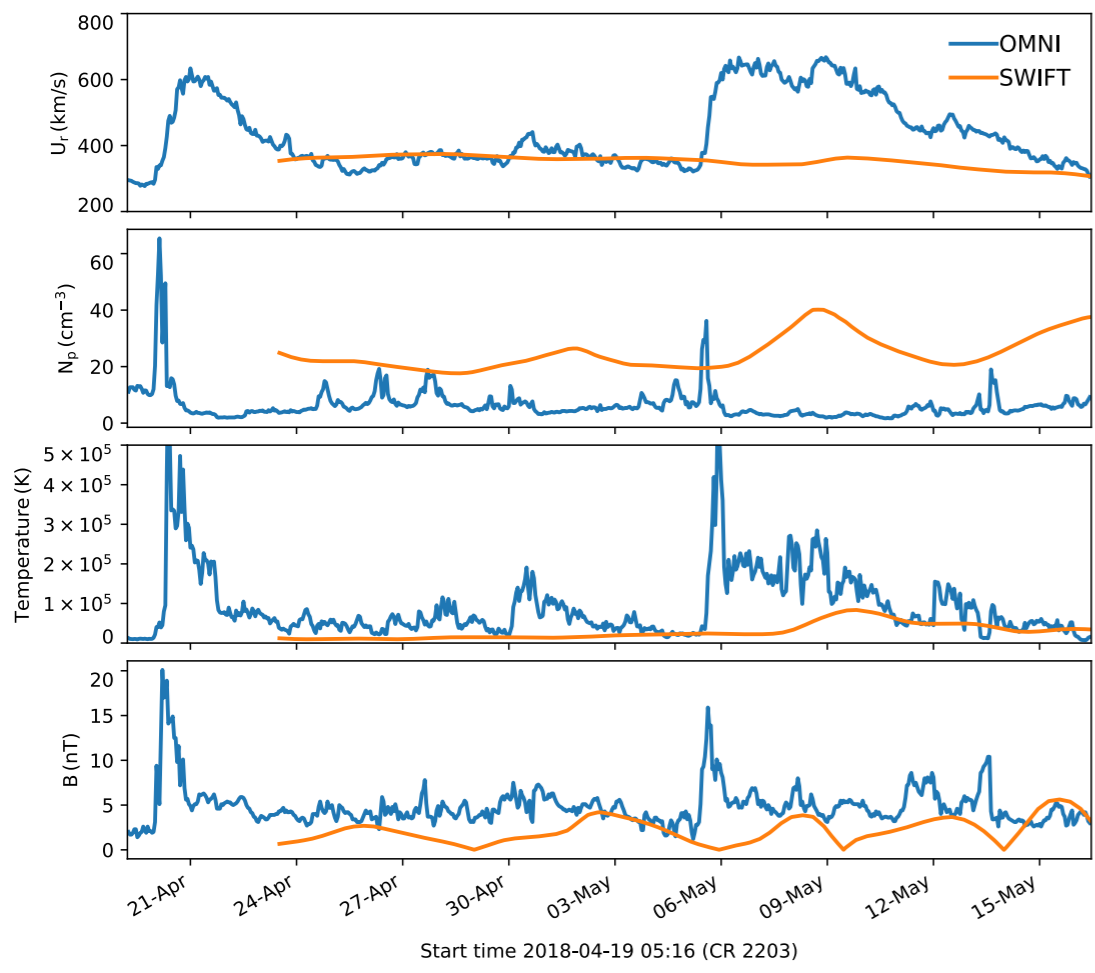


Only at real  $T_3$  can SWIFT time accurate simulations start  
These give time accurate answers from simulation time  $T_2$   
SWIFT simulations fast and continued after  $T_3$  with buffer fixed  
Start a new SWIFT run at  $T_4$  etc.

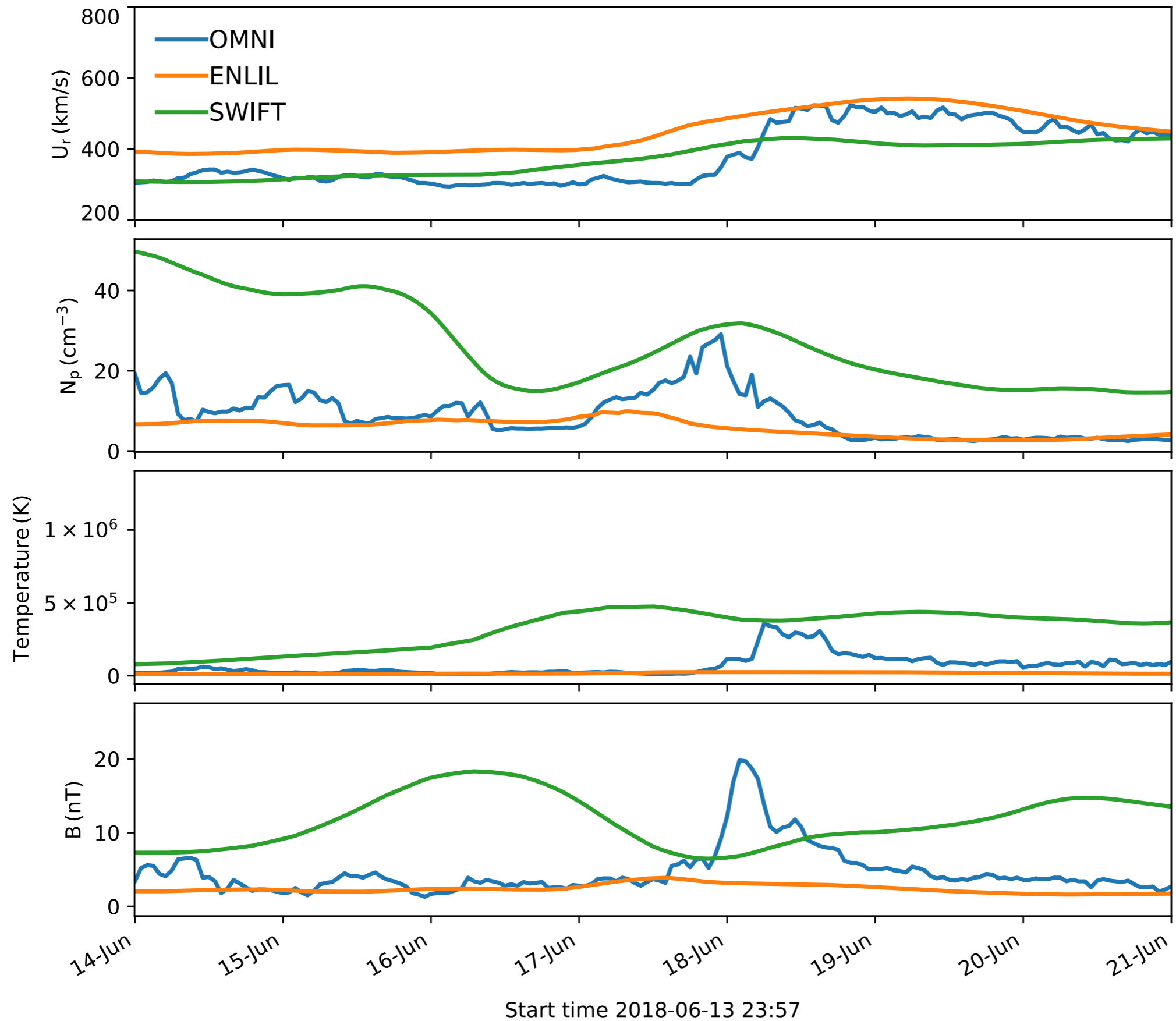


# AWSoM-SWIFT predictions

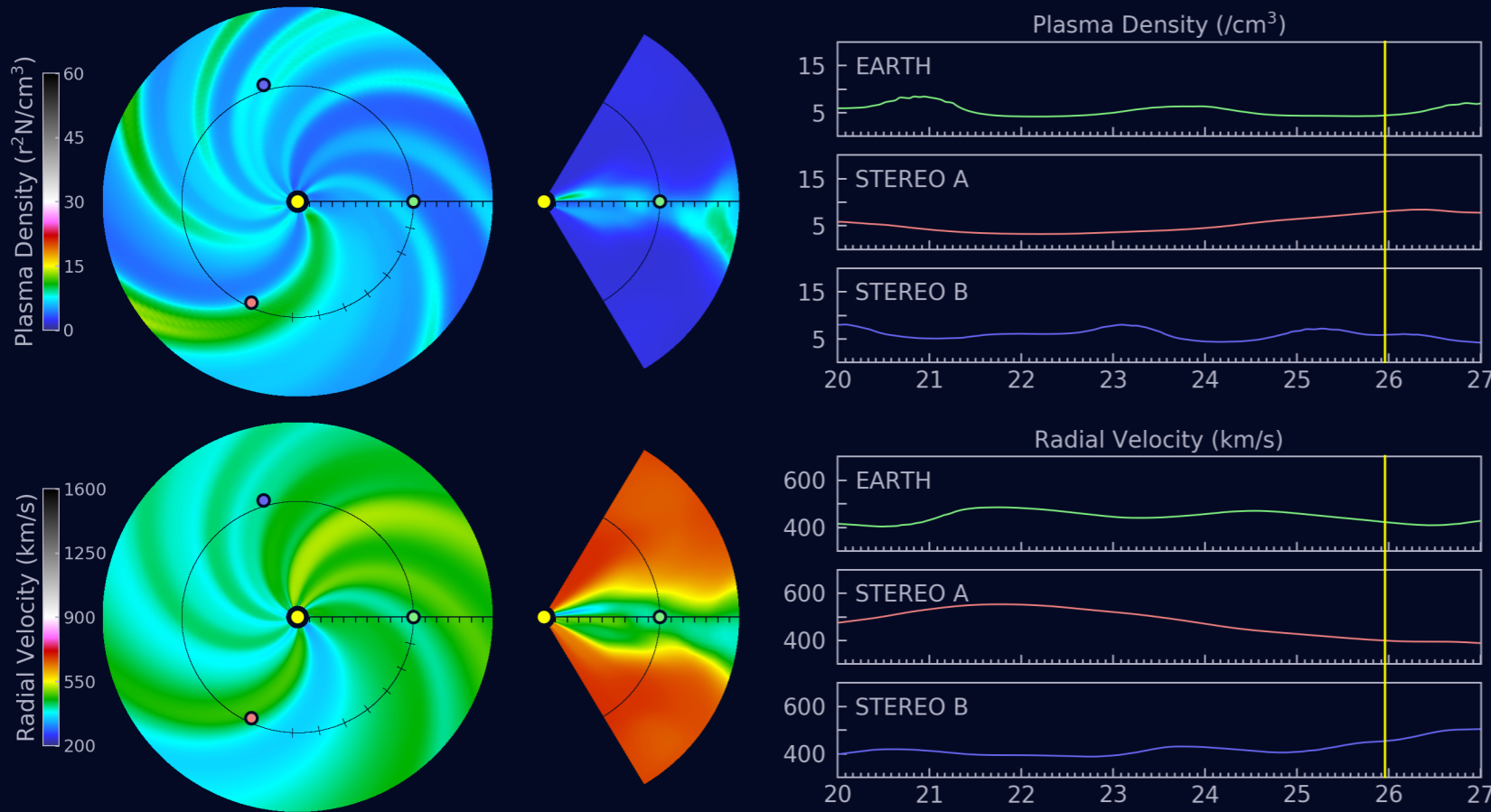




# AWSoM-SWIFT compared to ENLIL

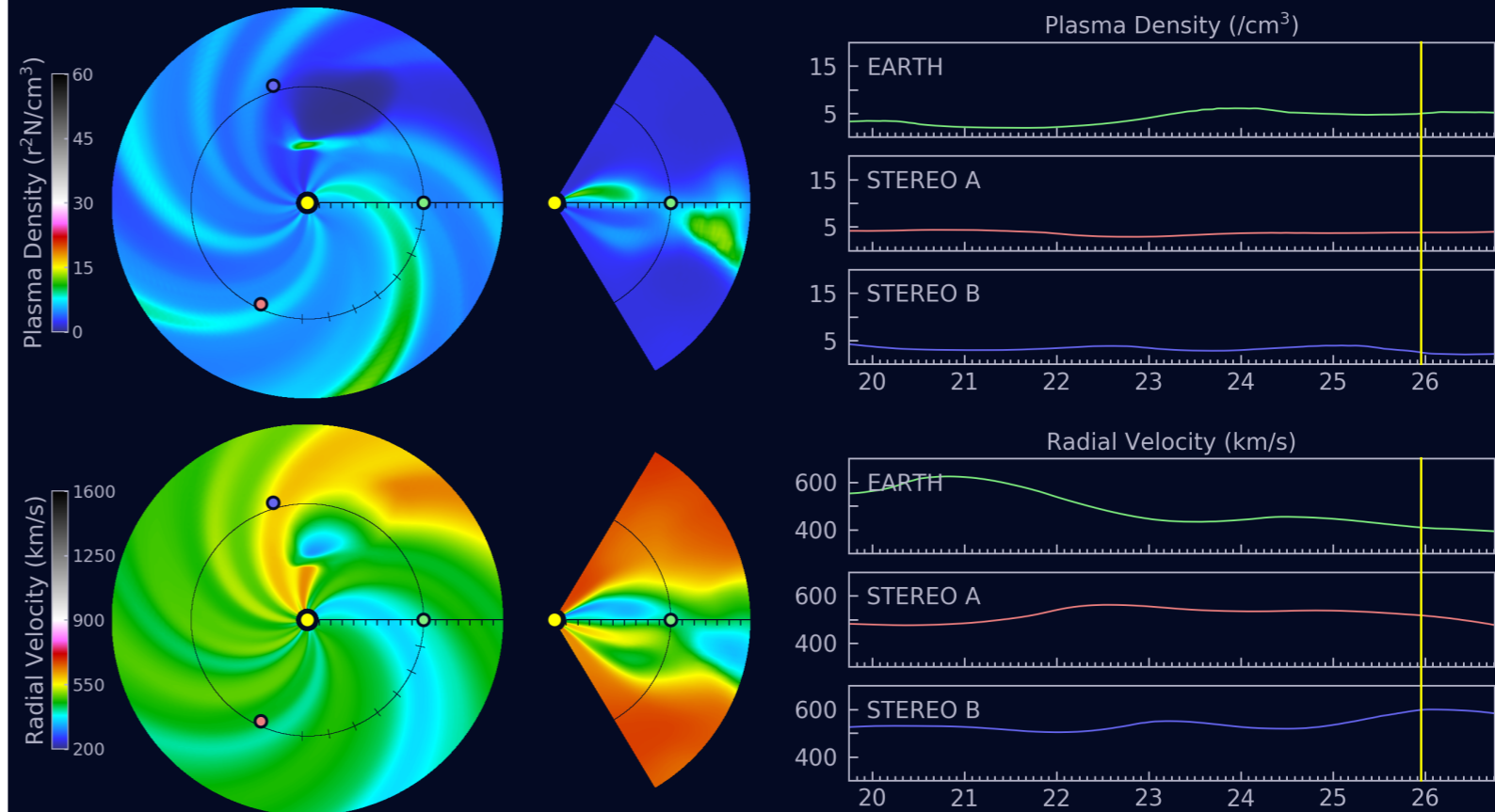


2018-06-25 23:00:00



**WSA-ENLIL vs  
WSA\_ENLIL Cone**

2018-06-25 23:00:00



# Summary

- AWSoM-SWIFT optimised for full Carrington rotation synoptic GONG magnetograms
- AWSoM speed improved by a factor  $\sim 100$
- Optimised codes now run on 32 cores in  $\sim 12$  hours
- Parallel conduction not traceable within fluid model, *ad hoc* limiter chosen over SNB
- Carrington fit 'good' but predictions from daily synoptic maps 'poor'
- Need long time base to test accuracy of predictions cf. WSA-ENLIL but initial visual inspection shows neither approach 'good' cf. Carrington rotation fits



